technische universität dortmund

fakultät für informatik

CS 12 computer science 12

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Exercise Sheet 3

(11 Punkte)

Exercise Due at Wednesday, April 29, 2015, 12:00 Uhr

Hinweise: Gruppenarbeit von bis zu drei Personen aus der gleichen Übungsgruppe ist möglich. Bitte vergessen Sie nicht Ihre Namen und Ihre Matrikelnummern auf die Lösung zu schreiben. **Die Abgaben können in den beschrifteten Briefkasten vor dem Sekretariat des LS12 (OH16/E22) eingeworfen oder per Mail (PDF Format) an georg.von-der-brueggen [☺] tu-dortmund.de abgegeben werden.**

Note: It is allowed to work in a group of up to three persons, if these persons are from the same practice group. Please do not forget to write your name and your Matrikelnummer on the solutions. **The solutions can either be placed in the mailbox in front of the secretary's office of LS 12 (OH/E22) or sent by mail (PDF format) to georg.von-der-brueggen [☺] tu-dortmund.de**

Exercise Sessions:
Do, 10:15 - 11:45   OH16/E18
Do, 14:15 - 15:45   OH16/E18

3.1   RM Scheduling (3 Punkte)

Suppose that we are given the following 3 sporadic real-time tasks with implicit deadlines.

	τ_1	τ_2	τ_3
C_i	1	2	3
T_i	4	6	10

1. What are their priority levels? Is the rate-monotonic (RM) schedule feasible?

2. What happens if we change the minimum inter-arrival time of task τ_3 from 10 to 8?

3.2   Different Schedulability Tests (2 Punkte)

What are the differences between the the efficient utilization-based schedulability tests and the time-demand schedulability tests for RM? Please use one example to illustrate their differences.

3.3   Optimality of RM (2 Punkte)

Explain how to use the time-demand analysis (TDA) to prove that rate-monotonic scheduling is an optimal static-priority scheduling policy (with respect to schedulability) for task systems with implicit deadlines.

Hint: Hint: You can prove by swapping two adjacent tasks (in the priority order) if they do not follow the RM scheduling policy. As long as the schedule after swapping the priority levels of these two tasks remains feasible, we can keep swapping the tasks to convert the order into RM such that the RM schedule remains feasible.

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3.4 Harmonic Task Systems (3 Punkte)

Given a set $\mathcal{T}$ of n independent, preemptable, and periodic tasks with implicit deadlines, they can be partitioned into $\mathcal{T}_1, \mathcal{T}_2, \ldots, \mathcal{T}_k$ task sets, in which $\bigcup_{j=1}^{k} \mathcal{T}_j$ is $\mathcal{T}$. Moreover, for $j = 1, 2, \ldots, k$, the periods of the tasks in each task set $\mathcal{T}_j$ are *simply periodic* or *harmonic*. That is, for any $\tau_i, \tau_\ell \in \mathcal{T}_j$, $\frac{T_i}{T_\ell}$ is a positive integer if $T_i \geq T_\ell$.

Prove that if

$$\sum_{i=1}^{n} U_i \leq k(2^{\frac{1}{k}} - 1),$$

rate-monotonic scheduling is a feasible schedule.

Hint: Hint: Convert these n tasks to a more difficult case with only k tasks.

3.5 Challenge (Optional Exercise with Bonus) (1 Punkt)

Mr. Smart suggests the following schedulability test of static-priority scheduling for sporadic real-time tasks, as defined in the course. He claims that task τ_i can meet its its relative deadline under the static-priority scheduling if and only if the following mixed-integer linear programming has a solution.

$$C_i + \sum_{j=1}^{i-1} n_j \cdot C_j \leq t \tag{1}$$

$$n_j \cdot T_j \geq t \qquad \forall j = 1, 2, \ldots, i-1 \tag{2}$$

$$n_j \in \mathbf{N} \qquad \forall j = 1, 2, \ldots, i-1 \tag{3}$$

$$0 < t \leq D_i, \tag{4}$$

where t is a positive variable, described in (4), and n_j is a positive integer number, described in (3). Please either explain/prove or disprove his argument.

General Hints: