Rechnerarchitektur SS 2020 Exercises: Energy and Power

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## Exercise - Voltage/Frequency Scaling

Suppose that we have to design a multiprocessor system to improve the energy efficiency of an application that was originally run on one processor with 1 GHz. The power consumption function when activating M processors at frequency f is

$$P(f) = 120 + M\left(10^4 \left(\frac{f}{1GHz}\right)^3 + 60\right) mWatt.$$

Please apply Amdahl's law.

What is the best number of processors to minimize the power consumption of the activated processors with the same performance as the original platform running at 1 GHz? What is the resulting power consumption?





# Exercise - Voltage/Frequency Scaling (cont.)

The power consumption function when activating M processors at frequency f is

$$P(f) = 120 + M\left(10^4 \left(\frac{f}{1GHz}\right)^3 + 60\right) mWatt.$$

Suppose that the application has 5% of its execution time that cannot be parallelized. The rest 95% of its execution time can be fully parallelized. What is the best number of processors to minimize the power consumption of the activated processors with the same performance as the original platform running at 1 GHz? What is the resulting power consumption?





# Exercise - Voltage/Frequency Scaling (cont.)

The power consumption function when activating M processors at frequency f is

$$P(f) = 120 + M\left(10^4 \left(\frac{f}{1GHz}\right)^3 + 60\right) mWatt.$$

Suppose that the application has x% of its execution time that cannot be parallelized. The rest (100-x)% of its execution time can be fully parallelized. What is the trend of the best number of processors to minimize the power consumption of the activated processors with respect to x when we would like to achieve the same performance as the original platform running at 1 GHz?

Hint: Try with x=0, 5, 10, 15, 20, 50.





Consider a micro-controller, which consumes  $P_{active} = 1.2mW$  in the ACTIVE/RUN mode or  $P_{sleep} = 0.1mW$  in the SLEEP mode. Regular activations of executions occur at times t = iT,  $i \in \{0, 1, 2, ...\}$  to interrupt and notify the processor about the arrival of new tasks. Each task needs to run  $t_{task}$  amount of time. The transition from the SLEEP mode to the ACTIVE/RUN mode lasts  $t_2$ ; the transition from the ACTIVE/RUN mode to the SLEEP mode lasts  $t_1$ . We assume that the micro-controller remains idle during these transitions. Also, for simplicity, we assume that the power changes continuously and linearly during the transitions. For the energy supply of the system, an energy source (battery) with 27 kJ is deployed.

source: Thiele, at ETHZ.



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1 Initially, neglect the transition times ( $t_1 = t_2 = 0$ ). Assume that after each interrupt, the processor gets into the ACTIVE mode and executes a task for  $t_{task} = 2$  sec. After the execution of the task, the processor returns into the SLEEP mode. Which condition must period *T* satisfy so that the system can execute at least  $10^7$  calculations (tasks)? How does this condition affect the maximum life time of the processor?





2 Next, assume that  $t_1 = 25$  ms,  $t_2 = 75$  ms,  $t_{task} = 100$  ms, and  $T = t_1 + t_2 + t_{task} = 200$  ms. At time t = 0 the processor is in SLEEP mode. Schedule **S1**: Transition to the ACTIVE mode follows directly after an interrupt. After the task execution, i.e., after ttask, the processor returns immediately to the SLEEP mode. Draw the schedule and analyze the energy consumption in the first 800 ms.





So Next, assume that  $t_1 = 25$  ms,  $t_2 = 75$  ms,  $t_{task} = 100$  ms, and  $T = t_1 + t_2 + t_{task} = 200$  ms. At time t = 0 the processor is in SLEEP mode. Schedule **S2**: If the processor is in the SLEEP mode when an interrupt occurs, then transition to the ACTIVE mode happens immediately. After the task execution, the processor decides whether to return to the SLEEP mode or to remain in the ACTIVE mode in order to execute the next task without delay when the next interrupt occurs. The processor makes this decision aiming at minimizing the energy consumption. Draw the schedule and analyze the energy consumption in the first 800 ms. Compute the energy difference, which can be saved on average per period T (200 ms) when Schedule **S2** is used instead of Schedule **S1**.



4 Next, assume that  $t_1 = 25$  ms,  $t_2 = 75$  ms,  $t_{task} = 100$  ms, and  $T = t_1 + t_2 + t_{task} = 200$  ms. Can we have better schedule (in terms of energy saving) than **S2** for which the following condition must hold: the task denoted by the i-th interrupt must have finished by the time the (i + 1)-th interrupt occurs?



