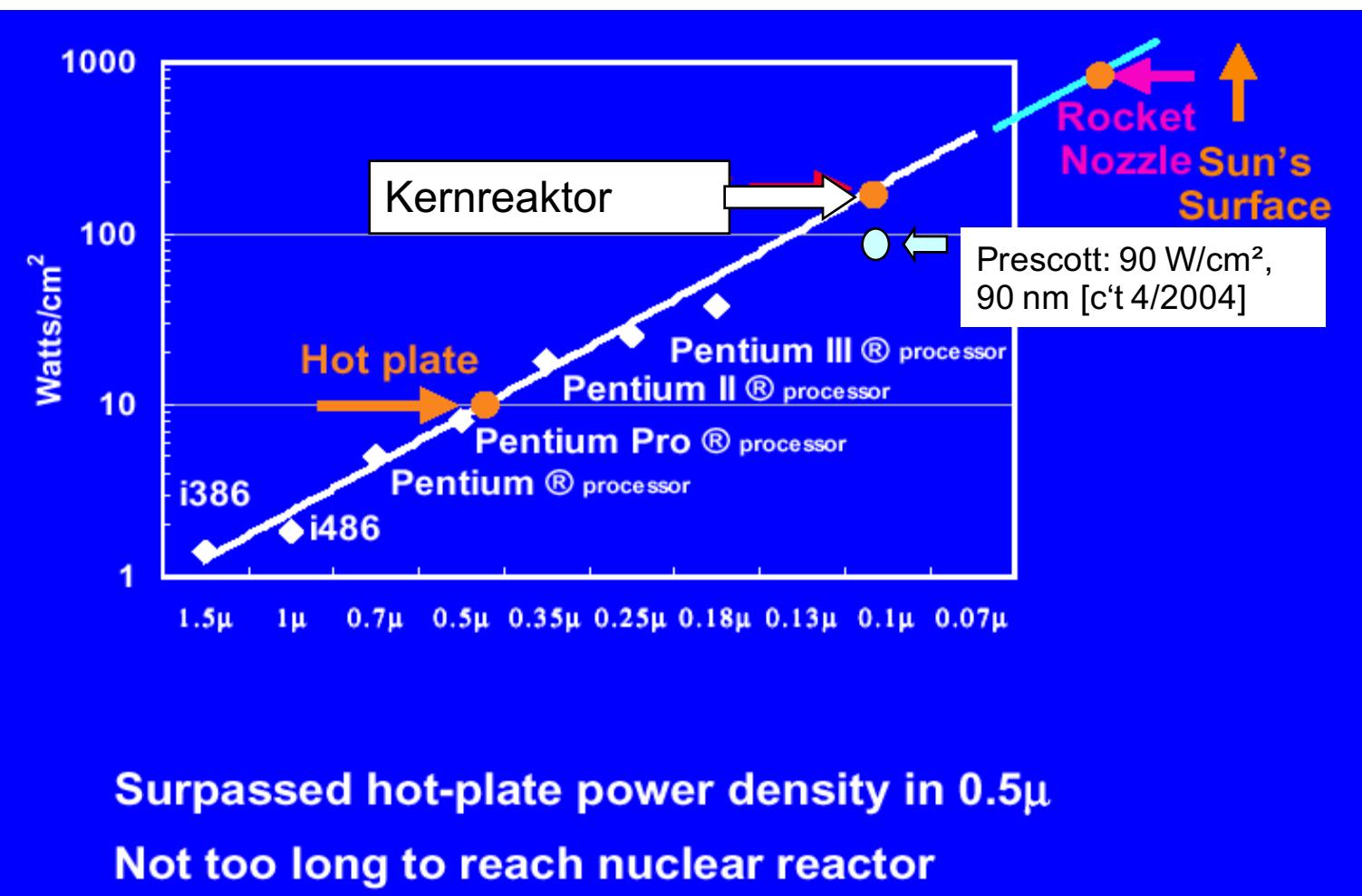


# Temperaturprobleme der modernen Rechnerarchitekturen

Basis:

- Pagani et al., DATE 2015, CODES+ISSS 2014
- Babak Falsafi: Dark Silicon & Its Implications on Server Chip Design, Microsoft Research, Nov. 2010  
Siehe auch *publications* unter <http://parsa.epfl.ch/~falsafi/>
- Hadi Esmaeilzadeh: Dark Silicon and the End of Multicore Scaling, International Symposium on Computer Architecture (ISCA '11)

# PCs: Leistungsdichte (Power density) steigt!!!!!!



© Intel  
M. Pollack,  
Micro-32

# PCs: Just adding transistors would have resulted in this:

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**Reuters: December 9, 2004:** Men should keep their laptops off their laps because they could damage fertility, an expert said on Thursday. Laptops, which reach **high internal operating temperatures, can heat up the scrotum which could affect the quality and quantity of men's sperm.** “The increase in scrotal temperature is significant enough to cause changes in sperm parameters,” said Dr Yefim Sheynkin, an associate professor of urology at the State University of New York at Stony Brook.



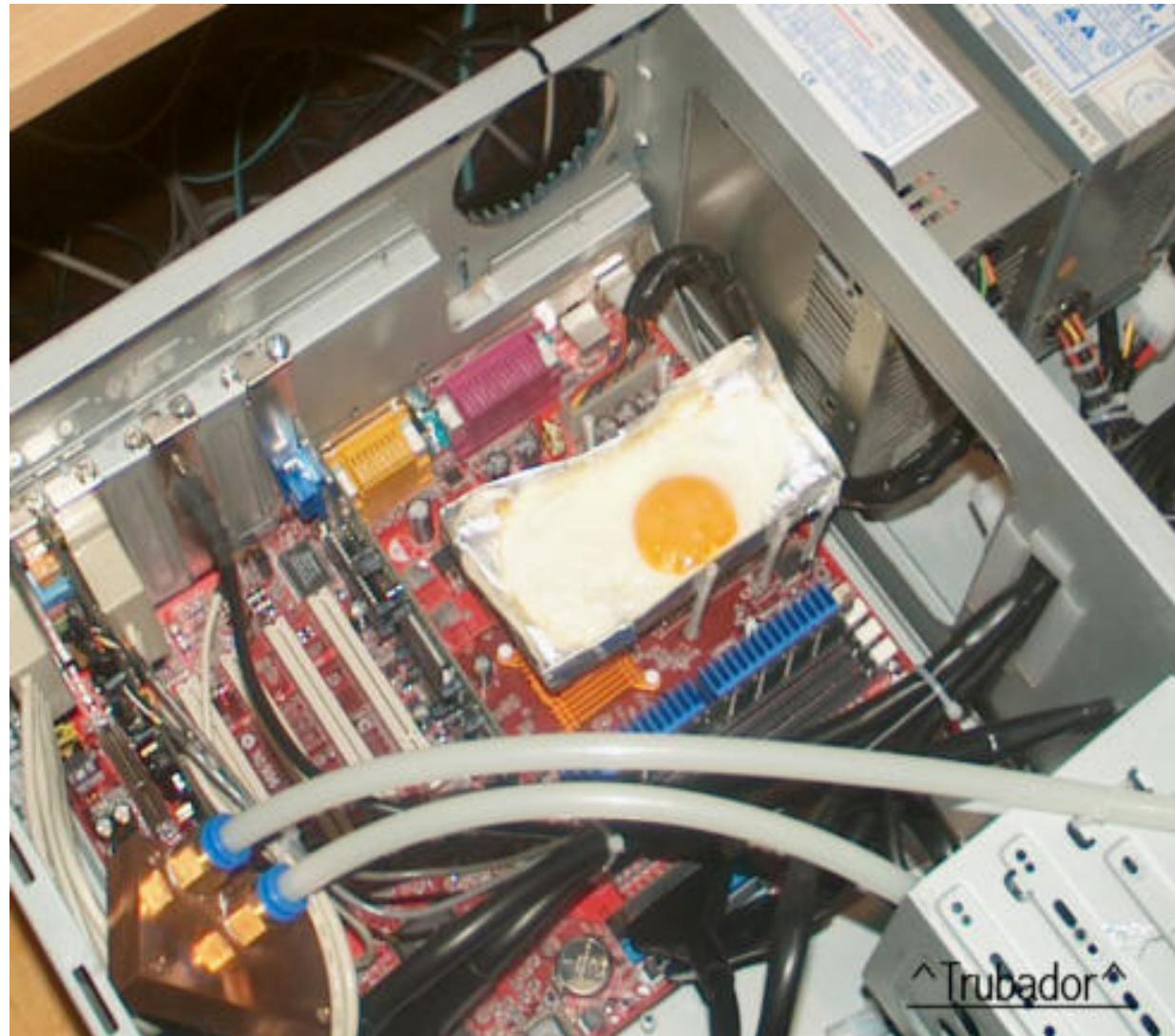
# Wie kochen wir?

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# PCs: Besser als Herdplatte ...? Warum nicht?

---



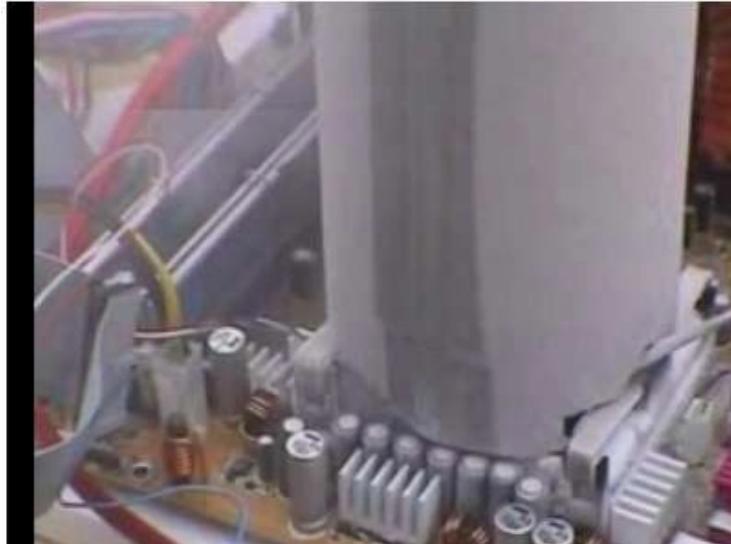
Strictly speaking, energy is not “consumed”, but converted from electrical energy into heat energy

[http://www.phys.ncku.edu.tw/~htsu/humor/fry\\_egg.html](http://www.phys.ncku.edu.tw/~htsu/humor/fry_egg.html)

# Verrückte Kühlungsmethode

---

- Thermoelektrische Kühlung
- Wasserkühlung
- Kältekühlung
- usw.



# Thermal Modeling: A Single Power Source

---

- Thermal conduction
  - Fourier's Law of Cooling: the temperature change is proportional to the difference of the chip and the ambient temperature (or the heat sink temperature)
    - If the chip is hotter, the temperature change drops more
    - If the chip is cooler, the temperature change drops less
  - Heating generation is proportional to the power consumption
    - If the power consumption is larger, the temperature change increases more
    - If the power consumption is smaller, the temperature change increases less
  - *Therefore,  $T'(t) = uP(t) - v(T(t)-T_{amb})$* 
    - $T(t)$  is the temperature of the power source at time  $t$
    - $P(t)$  is the power consumption of the power source at time  $t$
    - $T_{amb}$  is the ambient temperature. I will simple use it as 0. Why?
    - $u$  and  $v$  are both hardware-dependent constants.

# Solving Ordinary Differential Equation (ODE):

$$T'(t) = uP(t) - vT(t)$$

---

It is a standard linear ODE, where  $u$  and  $v$  are constants:

$$d \frac{T(t)e^{vt}}{dt} = e^{vt} d \frac{T(t)}{dt} + T(t) \cdot ve^{vt} = e^{vt}(uP(t) - vT(t)) + T(t) \cdot ve^{vt} = e^{vt}uP(t).$$

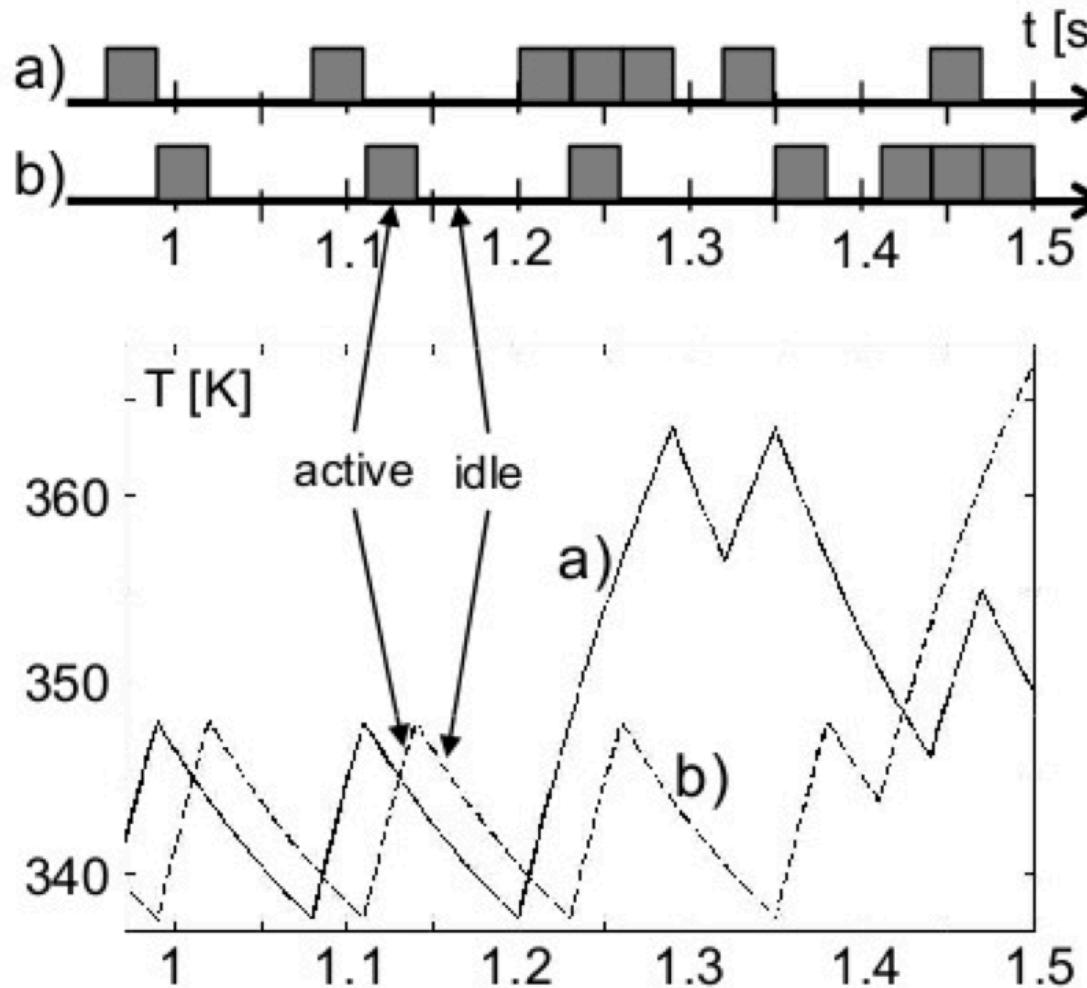
$$\int_{t_0}^t d \frac{T(t)e^{vt}}{dt} = \int_{t_0}^t e^{vt}uP(t) \Rightarrow T(t)e^{vt} - T(t_0)e^{vt_0} = \int_{t_0}^t e^{vx}uP(x)dx$$

$$\Rightarrow T(t) - T(t_0)e^{-v(t-t_0)} = \int_{t_0}^t e^{v(x-t)}uP(x)dx$$

$$\Rightarrow T(t) = T(t_0)e^{-v(t-t_0)} + \int_{t_0}^t e^{v(x-t)}uP(x)dx$$

- The temperature effect at time  $t_0$  decreases exponentially by  $T(t_0)e^{-v(t-t_0)}$ .
- The power consumption effect at time  $x$  decreases exponentially by  $T(t_0)e^{v(x-t)}$ , since  $v > 0$  and  $x - t \leq 0$  for  $x \leq t$ .

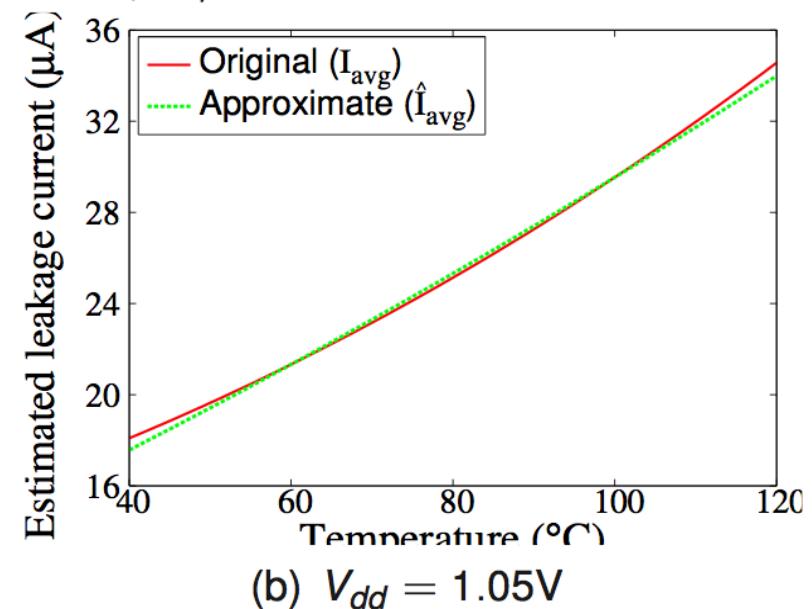
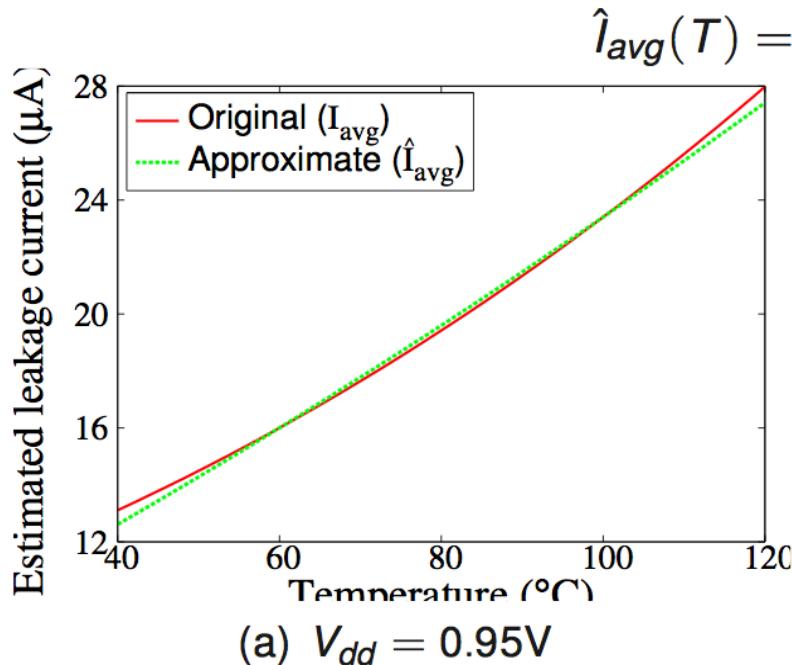
# Different Traces versus Temperature



# Thermal-Dependent Leakage Power Consumption

$$I_{avg}(T, V_{dd}) = I(T_0, V_0) \left( AT^2 e^{(\frac{q_1 \cdot V_{dd} + q_2}{T})} + Be^{(\gamma \cdot V_{dd} + \delta)} \right),$$

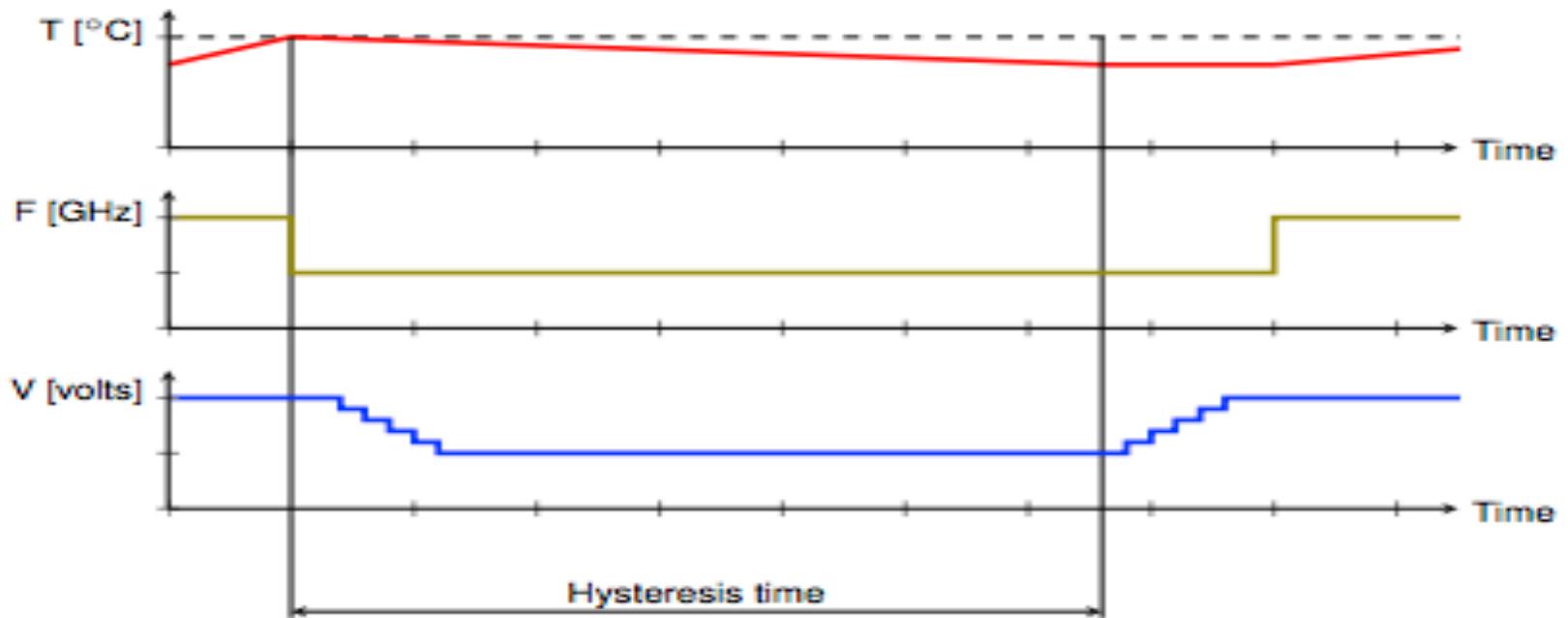
However, the term  $e^{(1/T)}$  dose not provide significant role in the accuracy. It is possible to use a simpler formula to formulate the leakage current.



Chuan-Yue Yang, Jian-Jia Chen, Lothar Thiele, Tei-Wei Kuo: Energy-efficient real-time task scheduling with temperature-dependent leakage. DATE 2010: 9-14

# Dynamic Thermal Management (DTM)

- Avoid possible over heating
  - DVFS
  - DPM



# Thermal Networks – Multiple Heat Sources

---

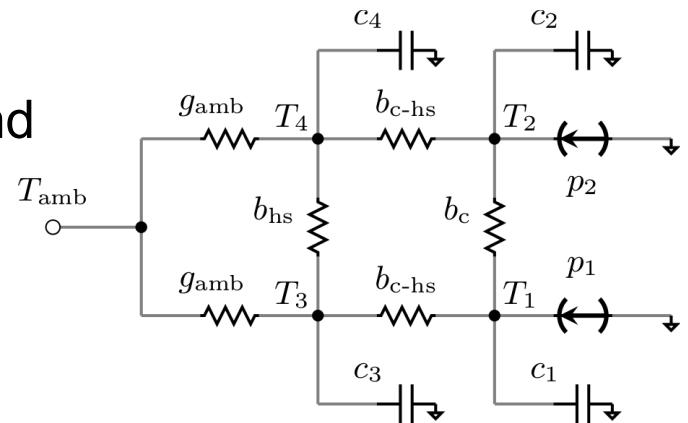
- Thermal models of applications depend on neighbouring cores.
  - A resistance-capacitance (RC) thermal network is widely used
    - A set of first order differential equations
  - Steady states (the equilibrium temperatures if the power does not change)
    - Simple linear algebra
  - Transient states (temperature profile in time)
    - Approximate the solution by using fourth-order *Runge-Kutta* numerical method [HotSpot, Huang et al. 2009]
    - Exact solution by using matrix exponential (**many approximations are available**) methods [MatEx, Pagani et al. to be published in DATE 2015]

[P.-Y. Huang and Y.-M. Lee, "Full-chip thermal analysis for the early design stage via generalized integral transforms," *IEEE Transactions on Very Large Scale Integration (VLSI) Systems*, vol. 17, no. 5, pp. 613–626, May 2009.]

[Santiago Pagani, Muhammad Shafique, Jian-Jia Chen and Jörg HenkelMatEx: Efficient Transient and Peak Temperature Computation for Compact Thermal Models in 18th Design, Automation & Test in Europe (DATE) 2015 ;]

# Thermal Model

- Thermal model → System of first-order differential equations
  - Relates temperature with power values and  $T_{amb}$
  - For example, RC thermal networks (like HotSpot)
- RC thermal network details



**Temperature Vectors**

$$\mathbf{AT}' + \mathbf{BT} = \mathbf{P} + T_{amb}\mathbf{G}$$

↑  
**Power Vector**

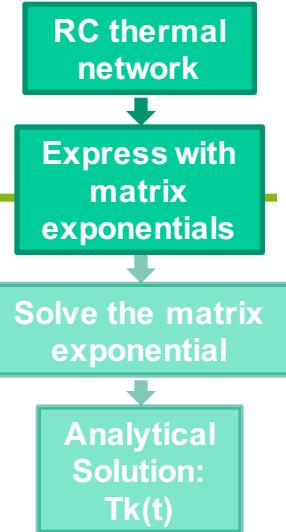
**Constant Matrices**      ↓  
 $\mathbf{A}$       ↓  
 $\mathbf{B}$

**Ambient Temperature**  
 $T_{steady} = \mathbf{B}^{-1}\mathbf{P} + T_{amb}\mathbf{B}^{-1}\mathbf{G}$

**Constant Vector**

# Computing Transient Temperatures

Thermal equation with matrix exponentials



Steady-State Temperatures  
(where vector  $\mathbf{T}$   
converges)

$$\mathbf{T} = \mathbf{T}_{\text{steady}} + e^{\mathbf{C}t}(\mathbf{T}_{\text{init}} - \mathbf{T}_{\text{steady}})$$

Matrix Exponential

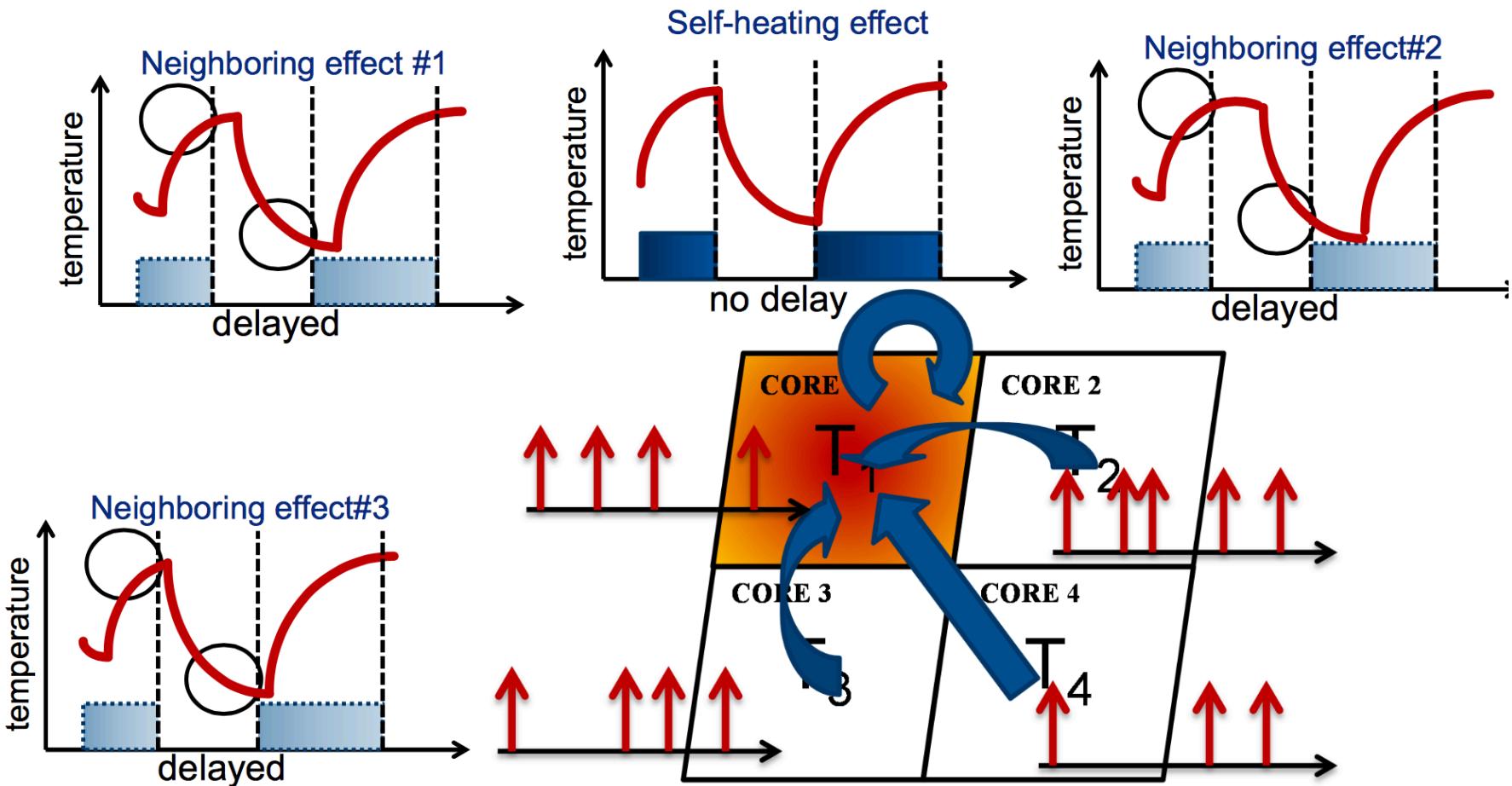
$$\mathbf{C} = -\mathbf{A}^{-1}\mathbf{B}$$

Initial Temperatures  
(at  $t = 0$ )

$$\mathbf{T}_{\text{steady}} = \mathbf{B}^{-1}\mathbf{P} + T_{\text{amb}}\mathbf{B}^{-1}\mathbf{G}$$

Pagani et al., DATE 2015

# Heat Transfer: Impulse Response

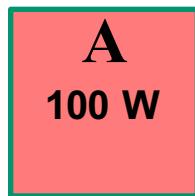


Thiele @ ETHZ

# The Dark Silicon Problem

So far: Constant power density

Tech. Node



$100 \text{ mm}^2$

$$\xrightarrow{\text{Scaling}} \frac{1 \text{ W/mm}^2}{1 \text{ W/mm}^2} = 1 \text{ W/mm}^2$$

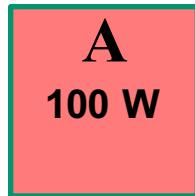
Tech. Node



OK  
 $50 \text{ mm}^2$

- Expected: Power density increases

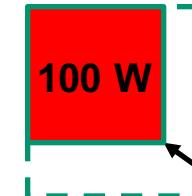
Tech. Node



$100 \text{ mm}^2$

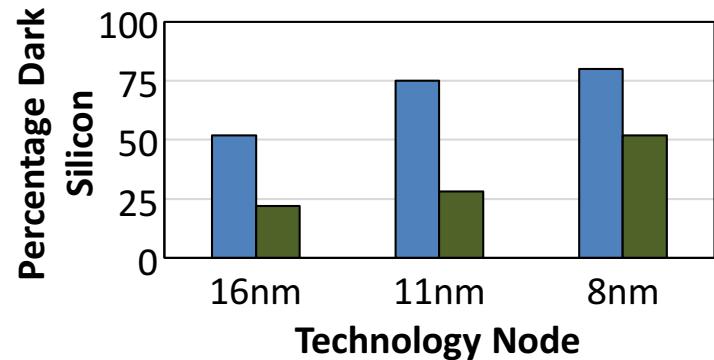
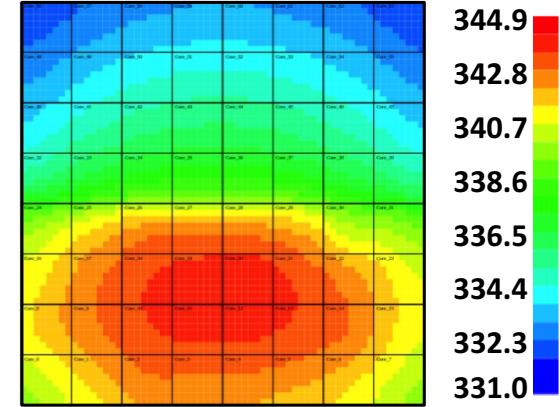
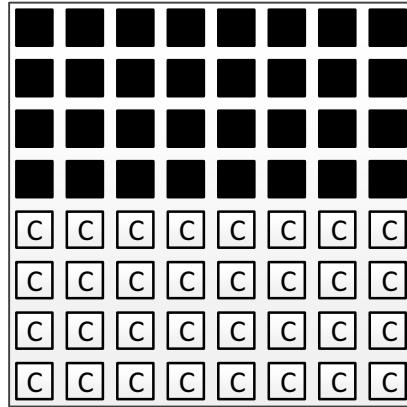
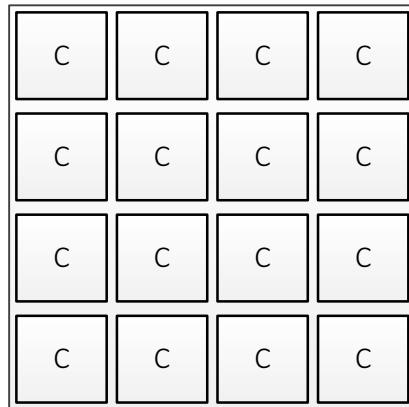
$$\xrightarrow{\text{Scaling}} \frac{1 \text{ W/mm}^2 < 2 \text{ W/mm}^2}{}$$

Tech. Node



$50 \text{ mm}^2$

# The Emerging Dark Silicon Problem



- [Blue square] Esmaeilzadeh@ISCA'11
- [Green square] Henkel, Shafique@DAC'15

# Caveat: Simple Parallelizable Workloads

Workloads are assumed parallel

- Scaling server workloads is reasonable

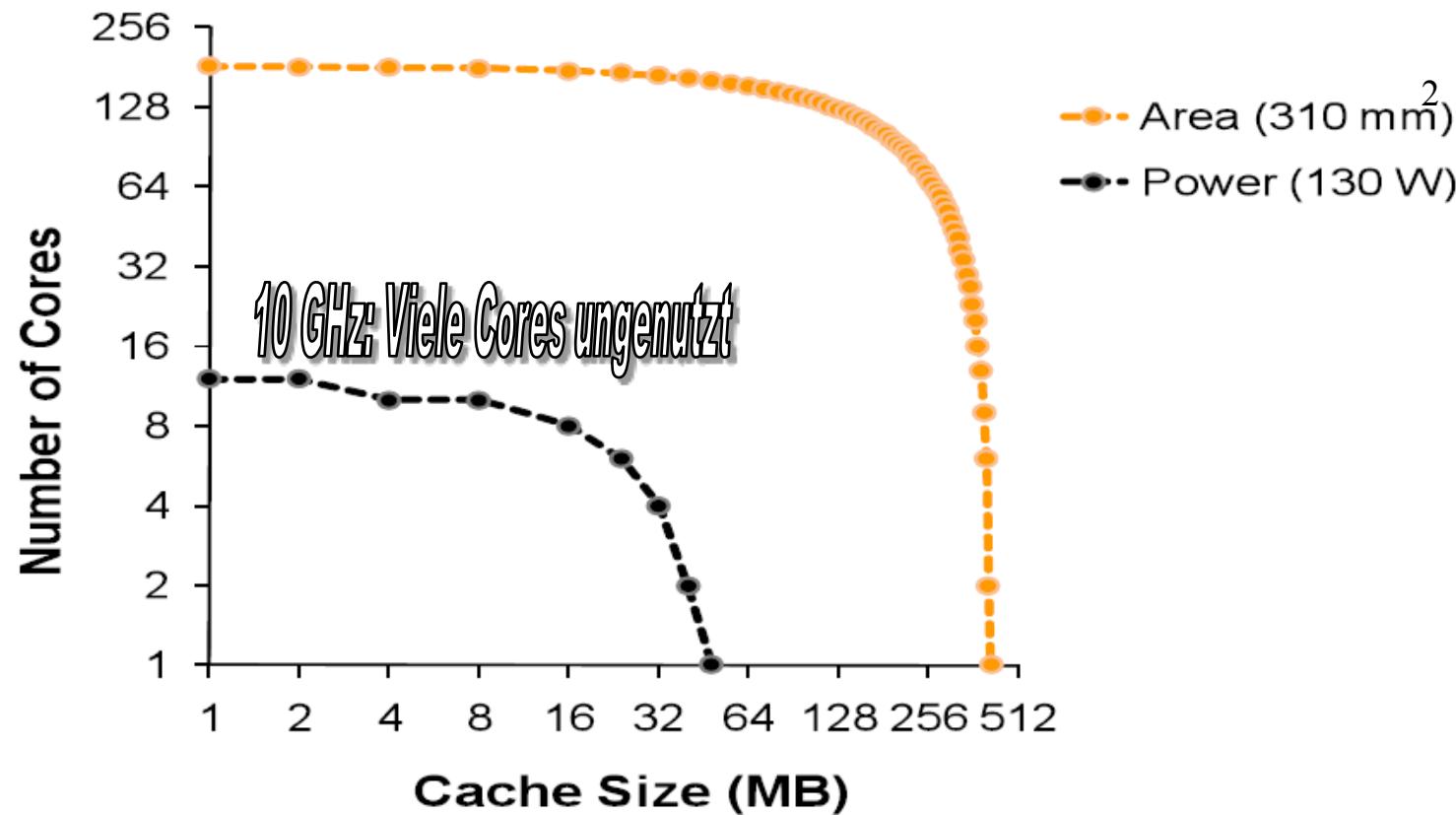
CPI model:

- Works well for workloads with low MLP
- OLTP, Web & DSS are mostly memory-latency dependent

Future servers will run a mix of workloads

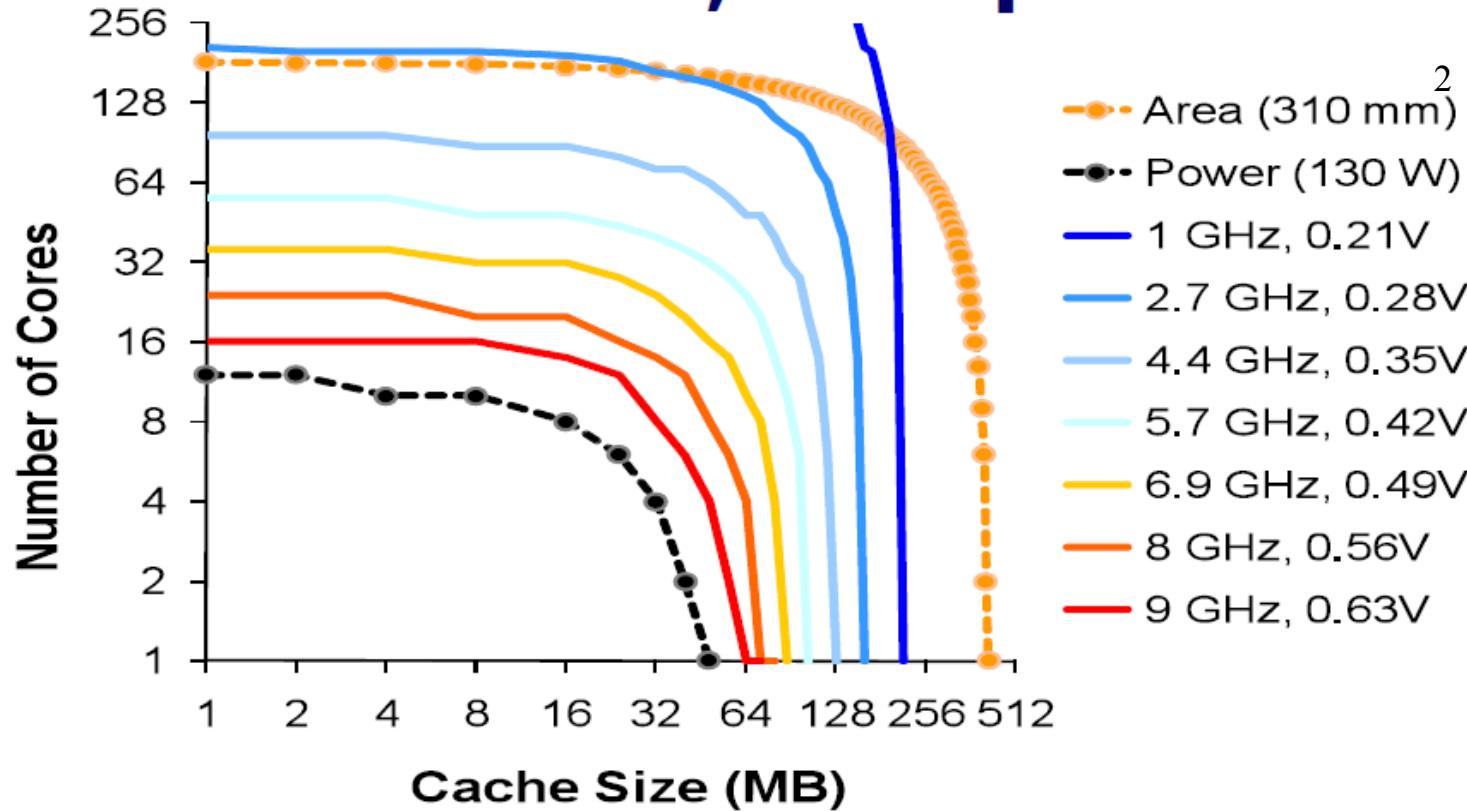
DSS=decision support system

# Area vs. Power Envelope (22nm)



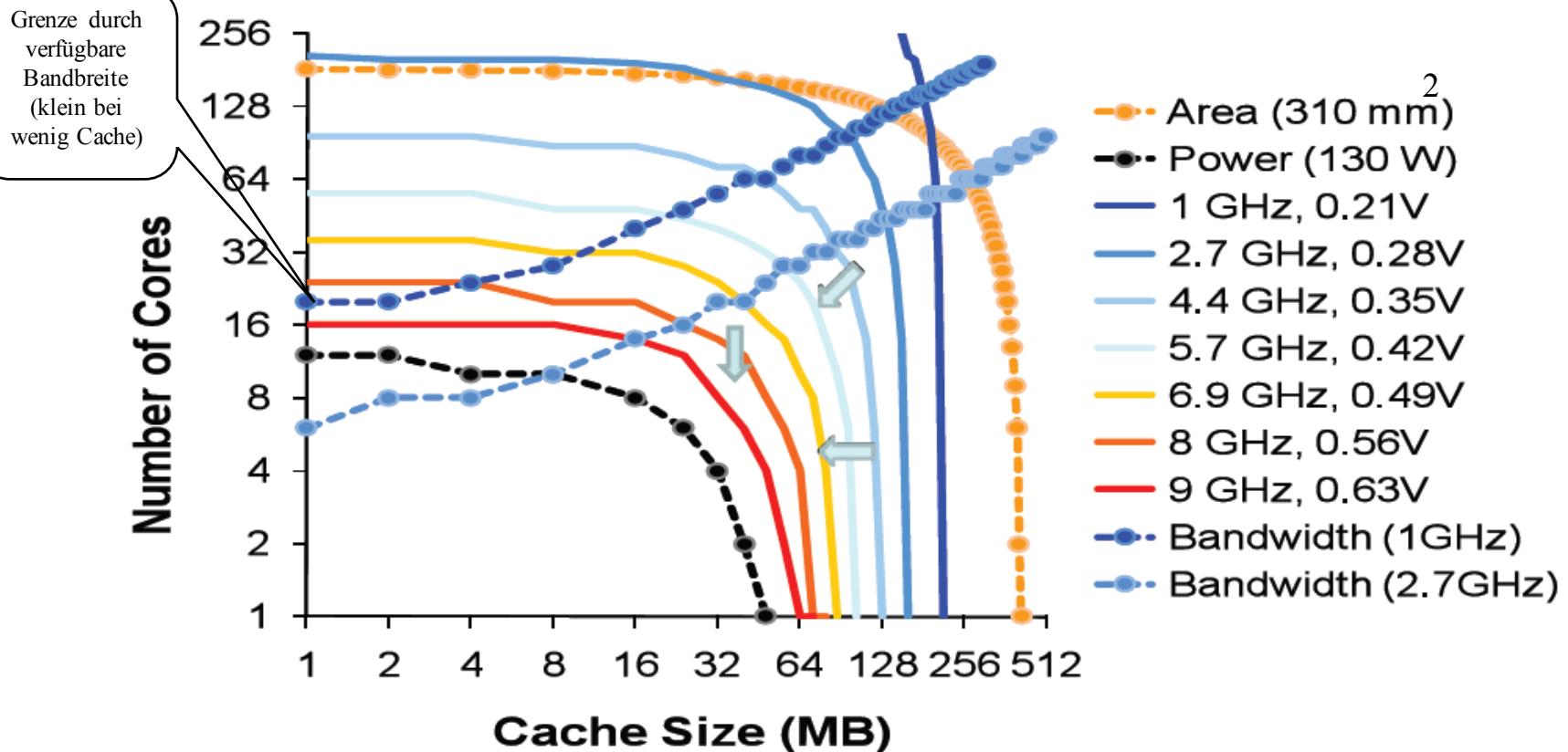
- ✓ Good news: can fit hundreds of cores
- ✗ Can not use them all at highest speed

# Of course one could pack more slower cores, cheaper cache



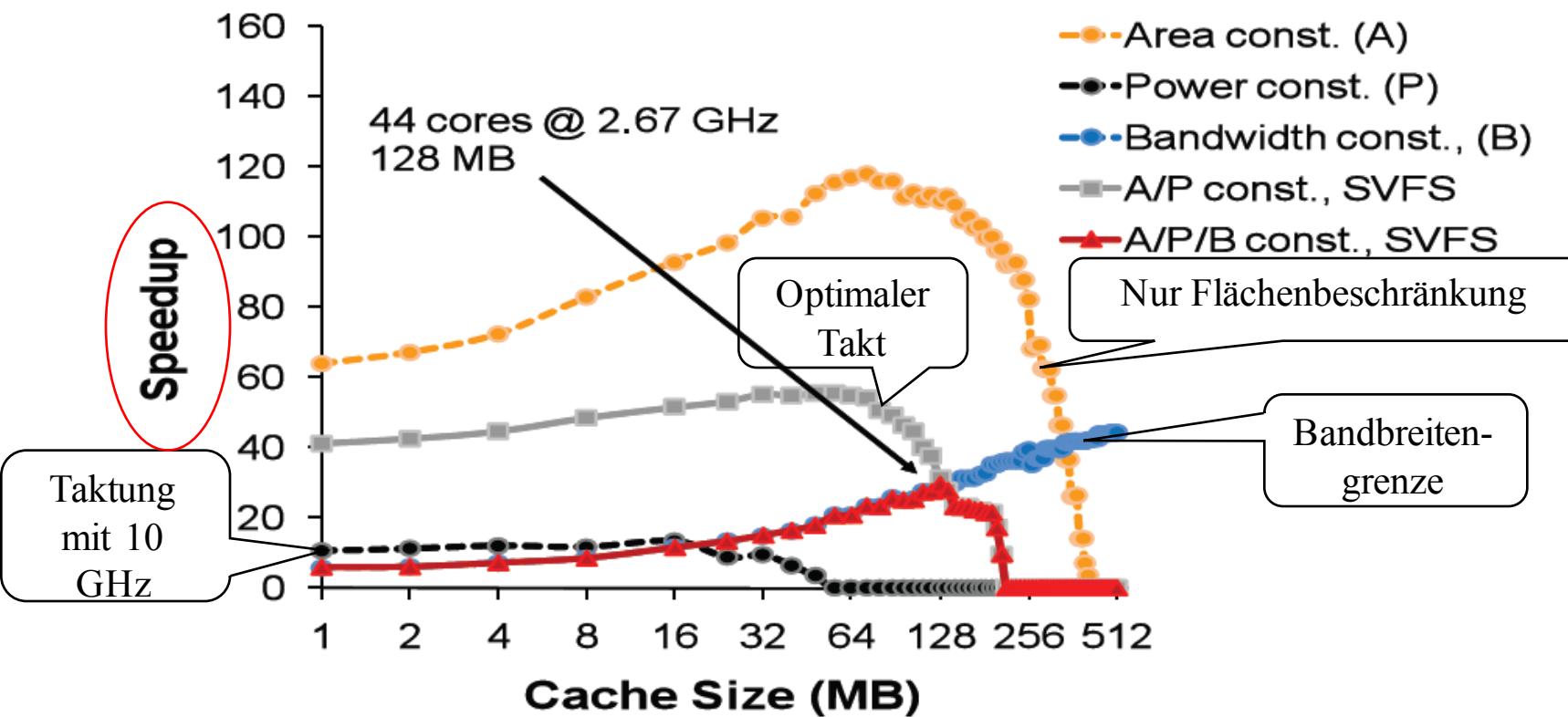
- Result: a performance/power trade-off
- Assuming bandwidth is unlimited

# But, limited pin b/w favors fewer cores + more cache



- For clarity, only showing two bandwidth lines
- Where would the best performance be?

# Peak Performing with Conventional Memory

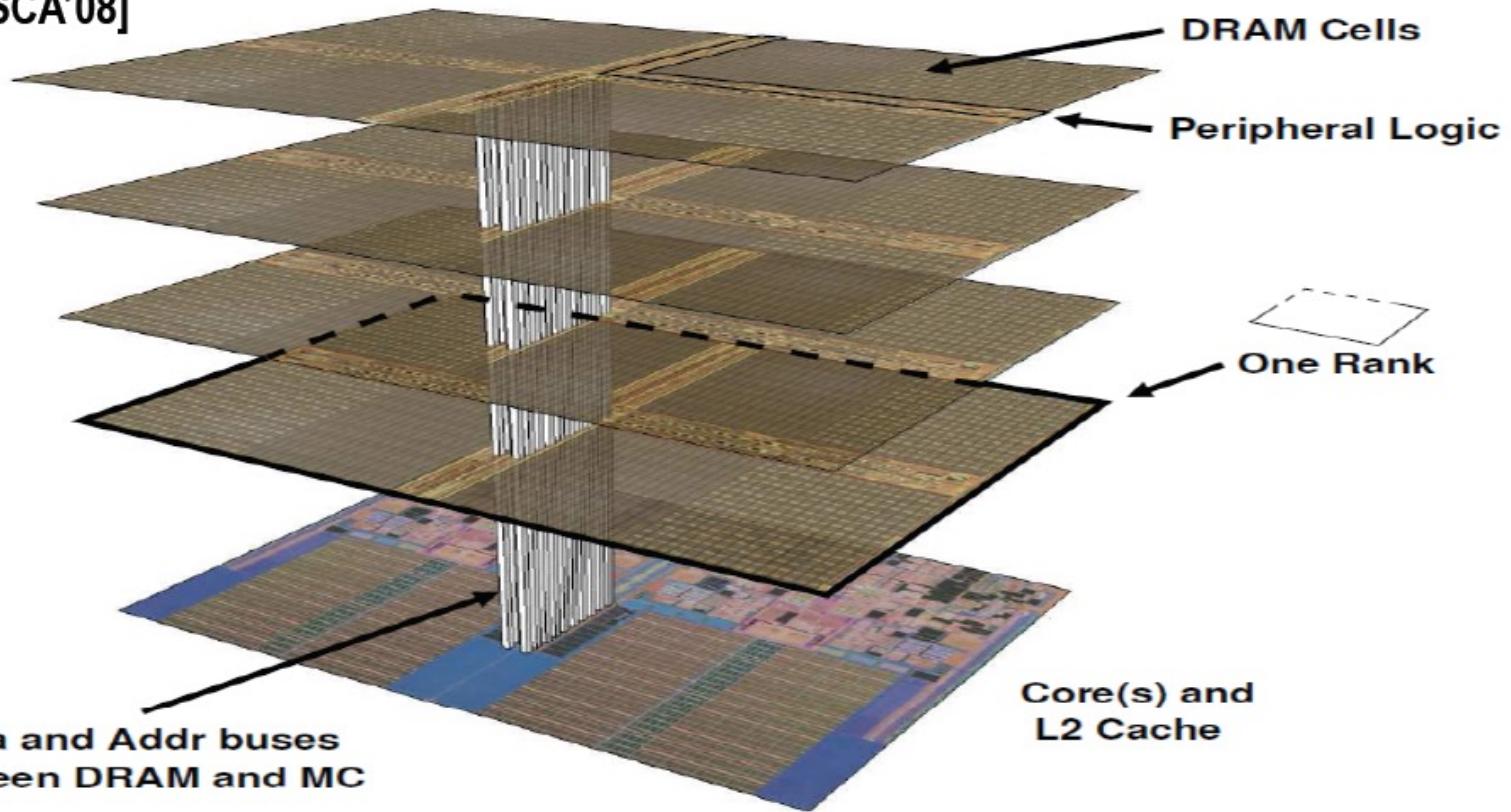


- B/W constrained, then power constrained
- Fewer slower cores, lots of cache

© 2010 Babak Falsafi

# Mitigating B/W Limitations: 3D-stacked Memory

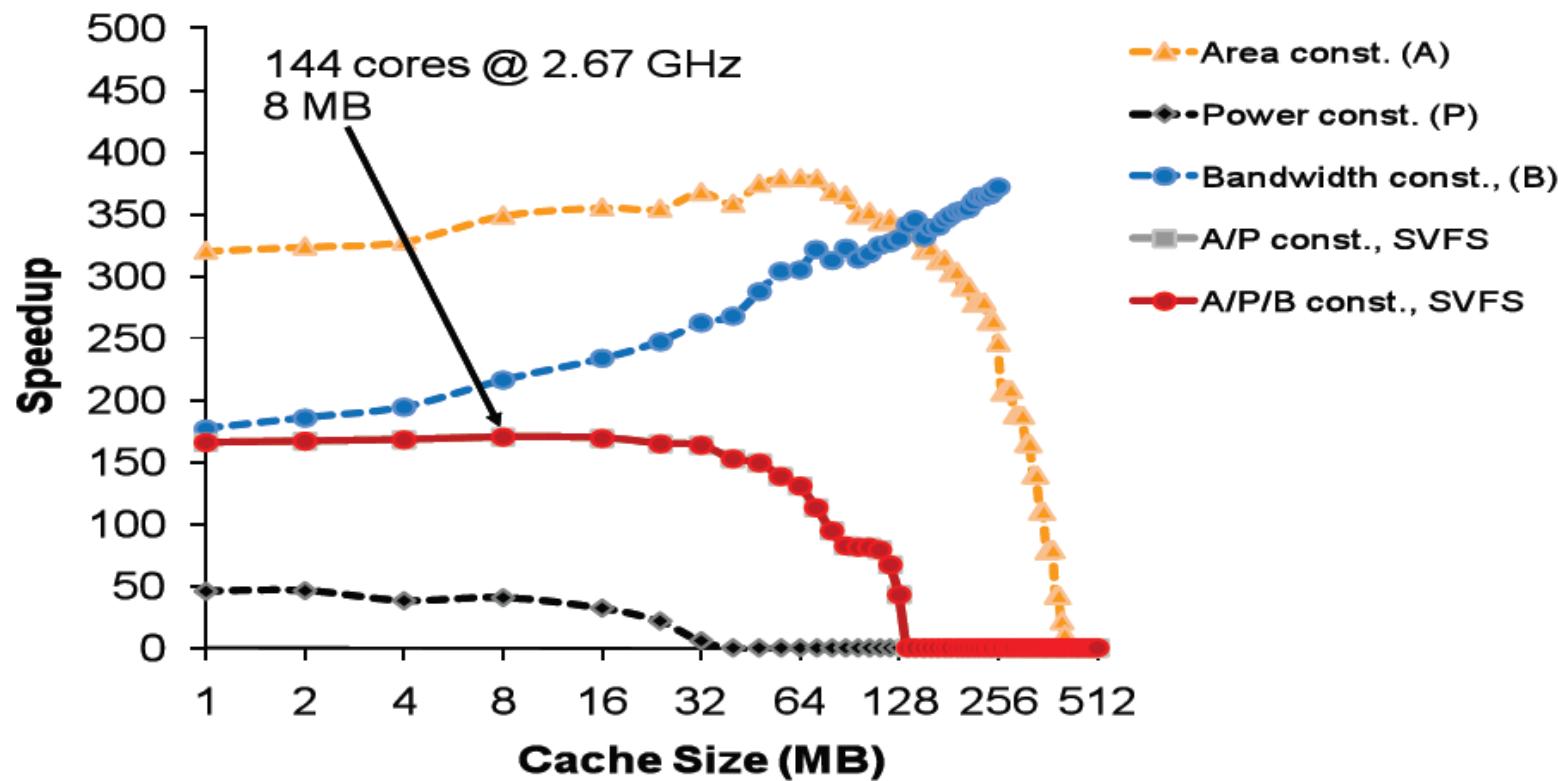
[Loh, ISCA'08]



- Delivers TB/sec of bandwidth

© 2010 Babak Falsafi

# Peak Performing w/ 3D-stacked Memory



- Only power-constrained
- Virtually eliminates on-chip cache

© 2010 Babak Falsafi

# Long-term: Where to go from here?

## 1. Redo SW stack

- Minimize joules/work (algo. down to HW)
- Program for locality + heterogeneity

## 2. Pray for technology

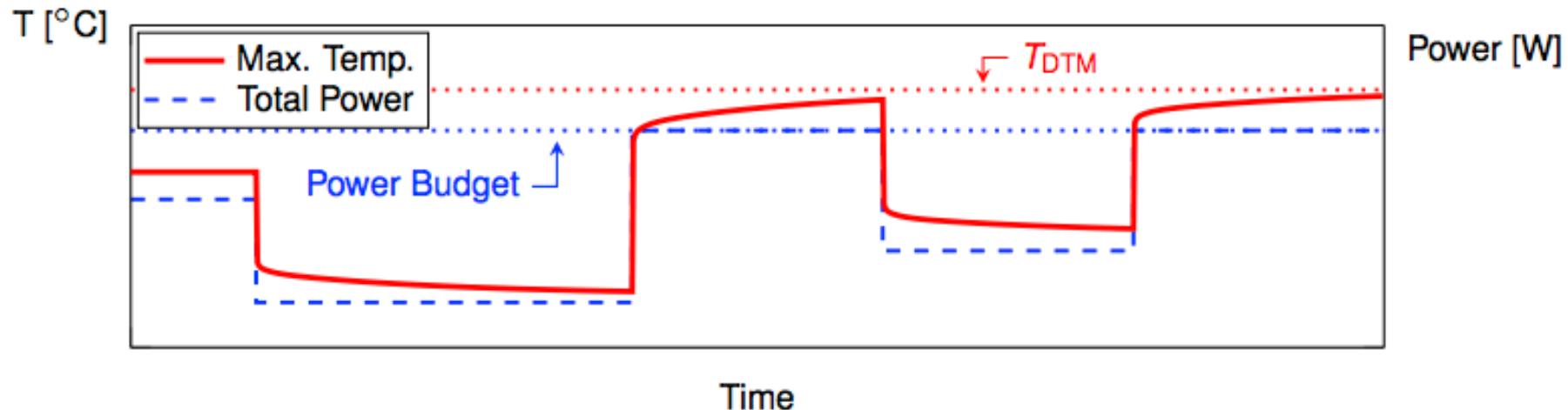
- Energy-scalable silicon devices
- Emerging nanoscale technologies?

## 3. Infrastructure technology

- Renewable/carbon-neutral energy
- Scalable cooling + power delivery

# Power Budget / Power Constraint

- Abstraction: Not deal directly with temperature.
- Generally, a power budget (for thermal safety) is a single value:
  - For each core (per-core).
  - For the entire chip (per-chip).

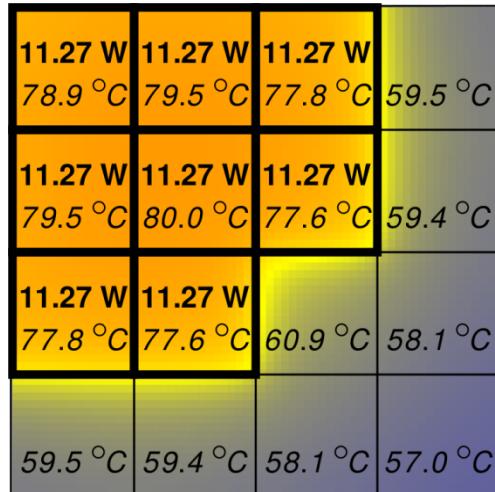


# Per-Chip / Per-Core Power Budgets

16 cores with area 5.3 mm<sup>2</sup>

Threshold temperature: 80°C

Power budget: 90 W



**8 active cores**

Highest Temperature: 80.0° C

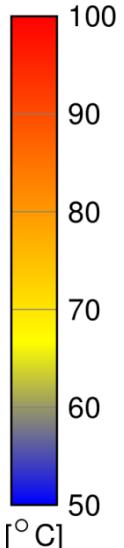
Highest Temperature: 86.3° C

Highest Temperature: 98.8C

**6 active cores**



**4 active cores**

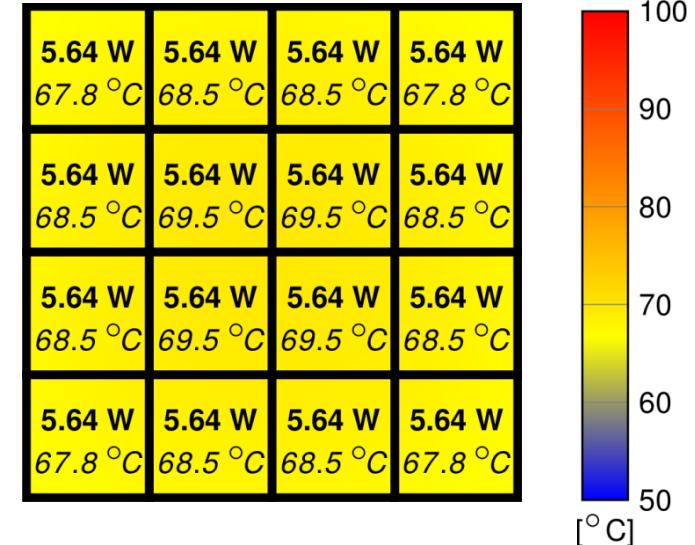
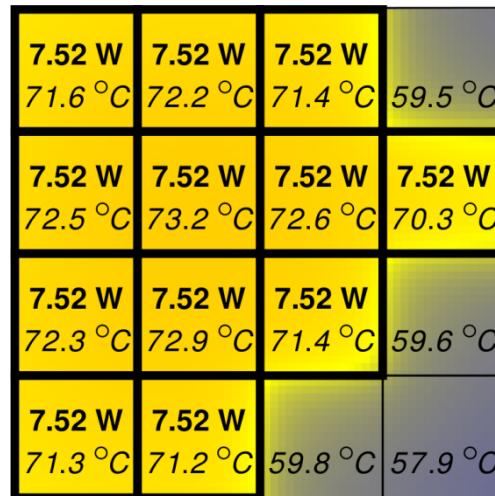
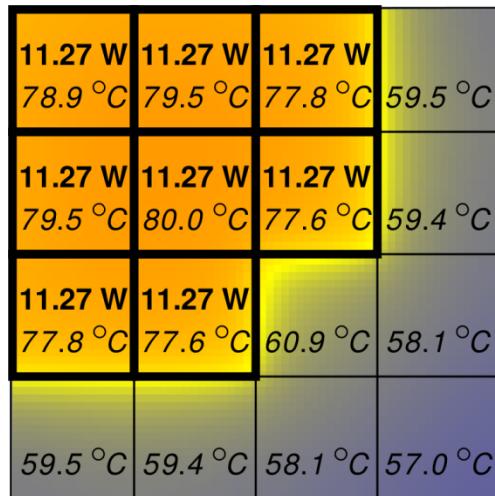


# Per-Chip / Per-Core Power Budgets

16 cores with area 5.3 mm<sup>2</sup>

Threshold temperature: 80°C

Power budget: 90 W



Highest Temperature: 80.0° C    Highest Temperature: 73.2° C    Highest Temperature: 69.5° C

8 active cores

12 active cores

16 active cores

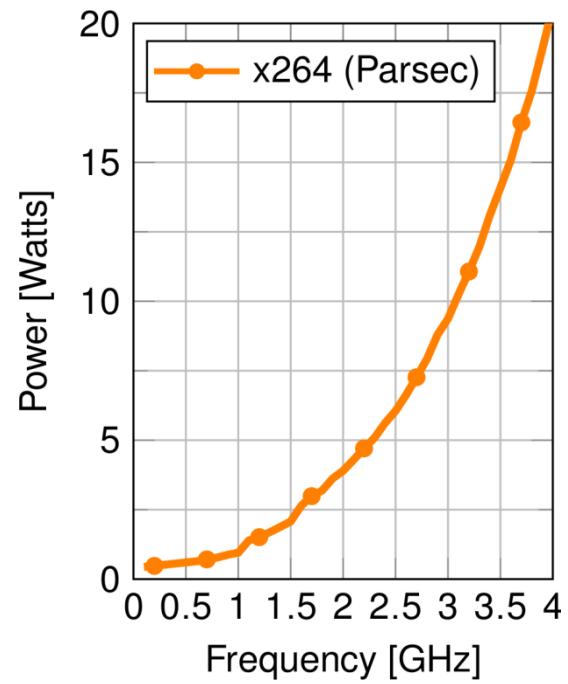
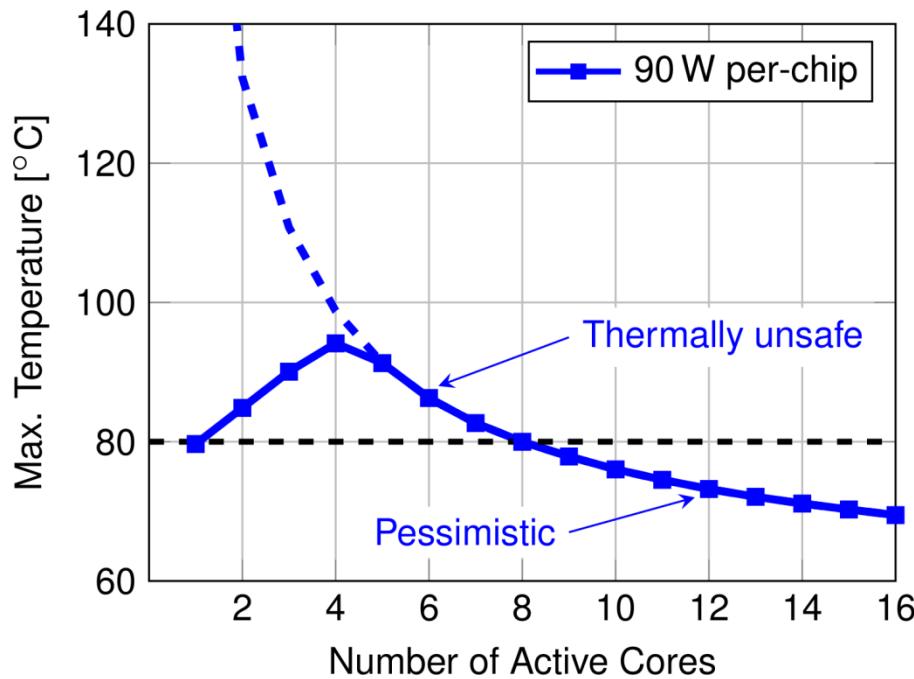
Pagani et al., CODES+ISSS 2014

# Problem with Per-Chip / Per-Core Power Budgets

16 cores with area  $5.3 \text{ mm}^2$

Threshold temperature for DTM:  $80^\circ\text{C}$

Power budget: 90 W



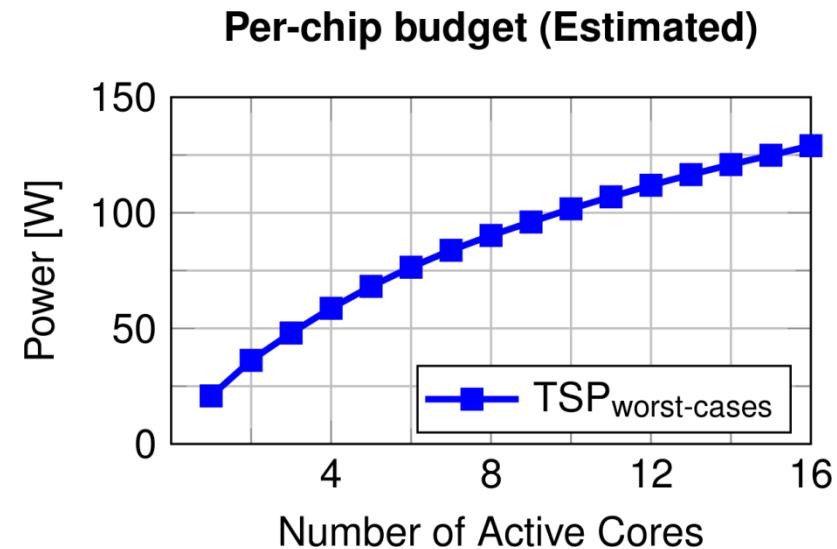
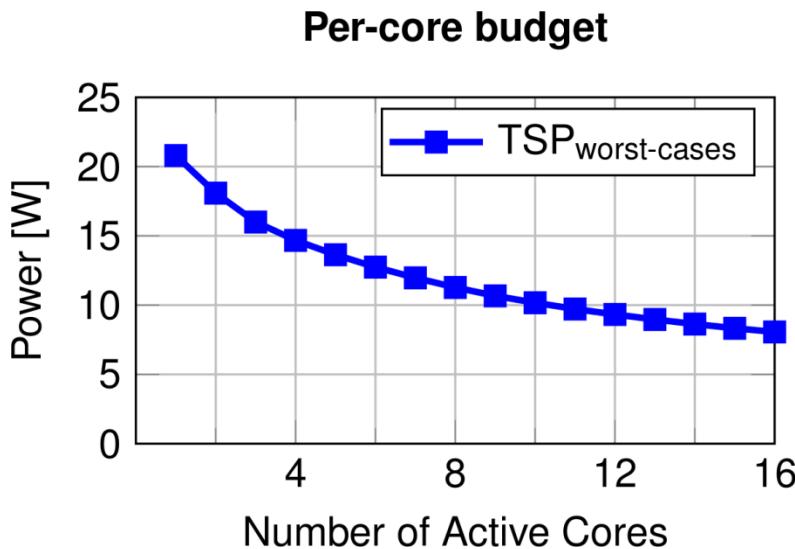
# Thermal Safe Power (TSP): Power Budget depending on # of activated cores

Power budget depends on the number of active cores

Safe for **any** 'm' active cores => Abstract mapping decisions

TSP table:

Active Cores	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
TSP per-core [W]	20.79	18.08	16.00	14.67	13.64	12.74	11.97	11.27	10.67	10.17	9.72	9.33	8.96	8.63	8.33	8.06



Pagani et al., CODES+ISSS 2014

# Cooling or Darkening Matters

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- Thermoelektrische Kühlung
- Wasserkühlung
- Kältekühlung
- usw.

