

# Evaluation and Validation

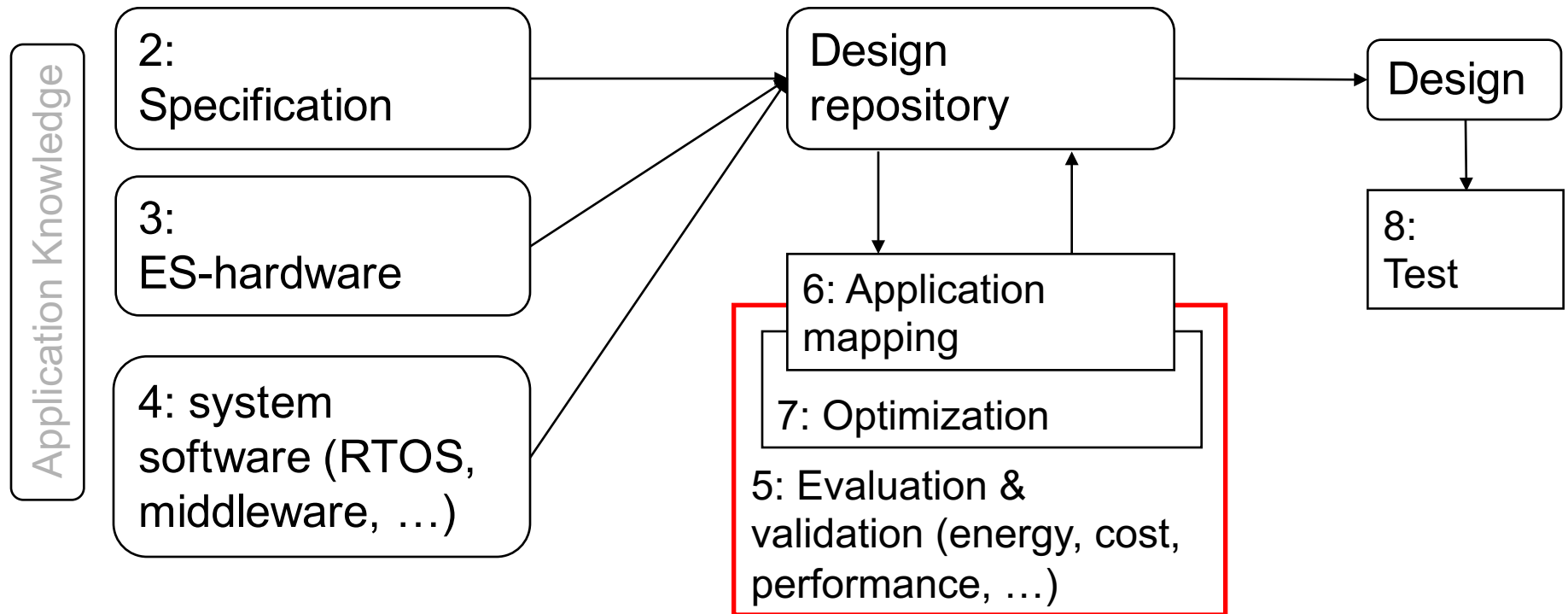
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(Slides are based on  
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# Structure of this course



Numbers denote sequence of chapters

# Validation and Evaluation

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**Definition:** Validation is the process of checking whether or not a certain (possibly partial) design is appropriate for its purpose, meets all constraints and will perform as expected (yes/no decision).

**Definition:** Validation with mathematical rigor is called (formal) verification.

**Definition:** Evaluation is the process of computing quantitative information of some key characteristics of a certain (possibly partial) design.

# How to evaluate designs according to multiple criteria?

Many different criteria are relevant for evaluating designs:

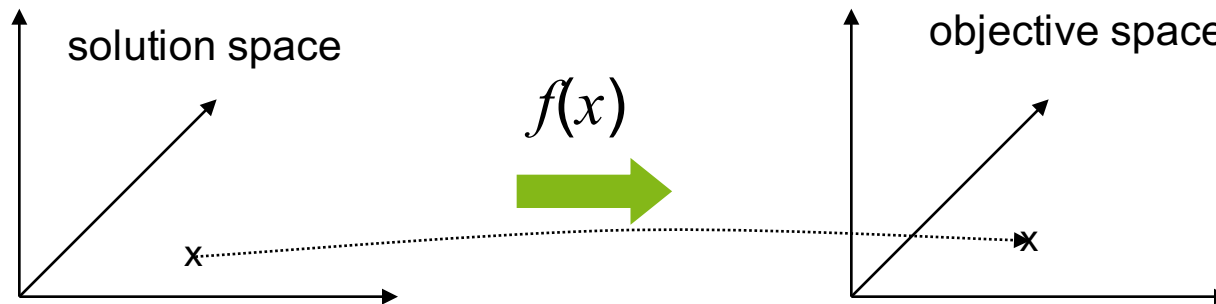
- Average & worst case delay
- power/energy consumption
- thermal behavior
- reliability, safety, security
- cost, size
- weight
- EMC characteristics
- radiation hardness, environmental friendliness, ..



How to compare different designs?  
(Some designs are “better” than others)

# Definitions

- Let  $X$ :  $m$ -dimensional **solution space** for the design problem.  
Example: dimensions correspond to # of processors, size of memories, type and width of busses etc.
- Let  $F$ :  $n$ -dimensional **objective space** for the design problem.  
Example: dimensions correspond to average and worst case delay, power/energy consumption, size, weight, reliability, ...
- Let  $f(x) = (f_1(x), \dots, f_n(x))$  where  $x \in X$  be an **objective function**.  
We assume that we are using  $f(x)$  for evaluating designs.



# Pareto points

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- We assume that, for each objective, an order  $<$  and the corresponding order  $\leq$  are defined.

- **Definition:**

Vector  $u=(u_1, \dots, u_n) \in F$  **dominates** vector  $v=(v_1, \dots, v_n) \in F$

$\Leftrightarrow$

$u$  is “better” than  $v$  with respect to *at least* one objective and not worse than  $v$  with respect to all other objectives:

$$\forall i \in \{1, \dots, n\} : u_i \leq v_i \wedge$$

$$\exists i \in \{1, \dots, n\} : u_i < v_i$$

- **Definition:**

Vector  $u \in F$  is **indifferent** with respect to vector  $v \in F$

$\Leftrightarrow$  neither  $u$  dominates  $v$  nor  $v$  dominates  $u$

# Pareto points

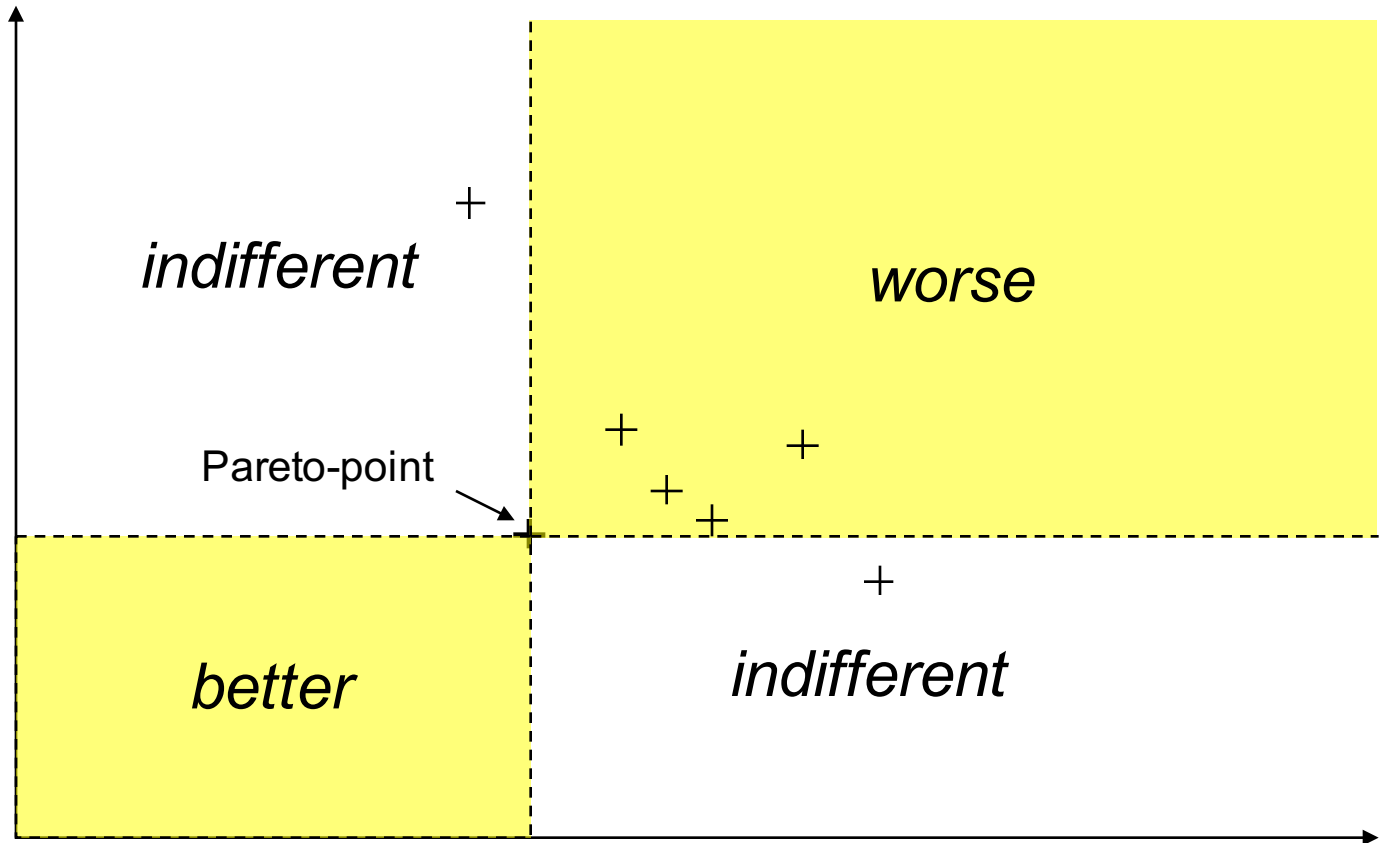
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- A solution  $x \in X$  is called **Pareto-optimal** with respect to  $X$   
 $\Leftrightarrow$  there is no solution  $y \in X$  such that  $u=f(x)$  is dominated by  $v=f(y)$ .  $x$  is a **Pareto point**.
- **Definition:** Let  $S \subseteq F$  be a subset of solutions.  
 $v \in F$  is called a **non-dominated solution** with respect to  $S$   
 $\Leftrightarrow v$  is not dominated by any element  $\in S$ .
- $v$  is called **Pareto-optimal**  
 $\Leftrightarrow v$  is non-dominated with respect to all solutions  $F$ .
- A **Pareto-set** is the set of all Pareto-optimal solutions

Pareto-sets define a **Pareto-front**  
(boundary of dominated subspace)

# Pareto Point

Objective 1  
(e.g. energy consumption)



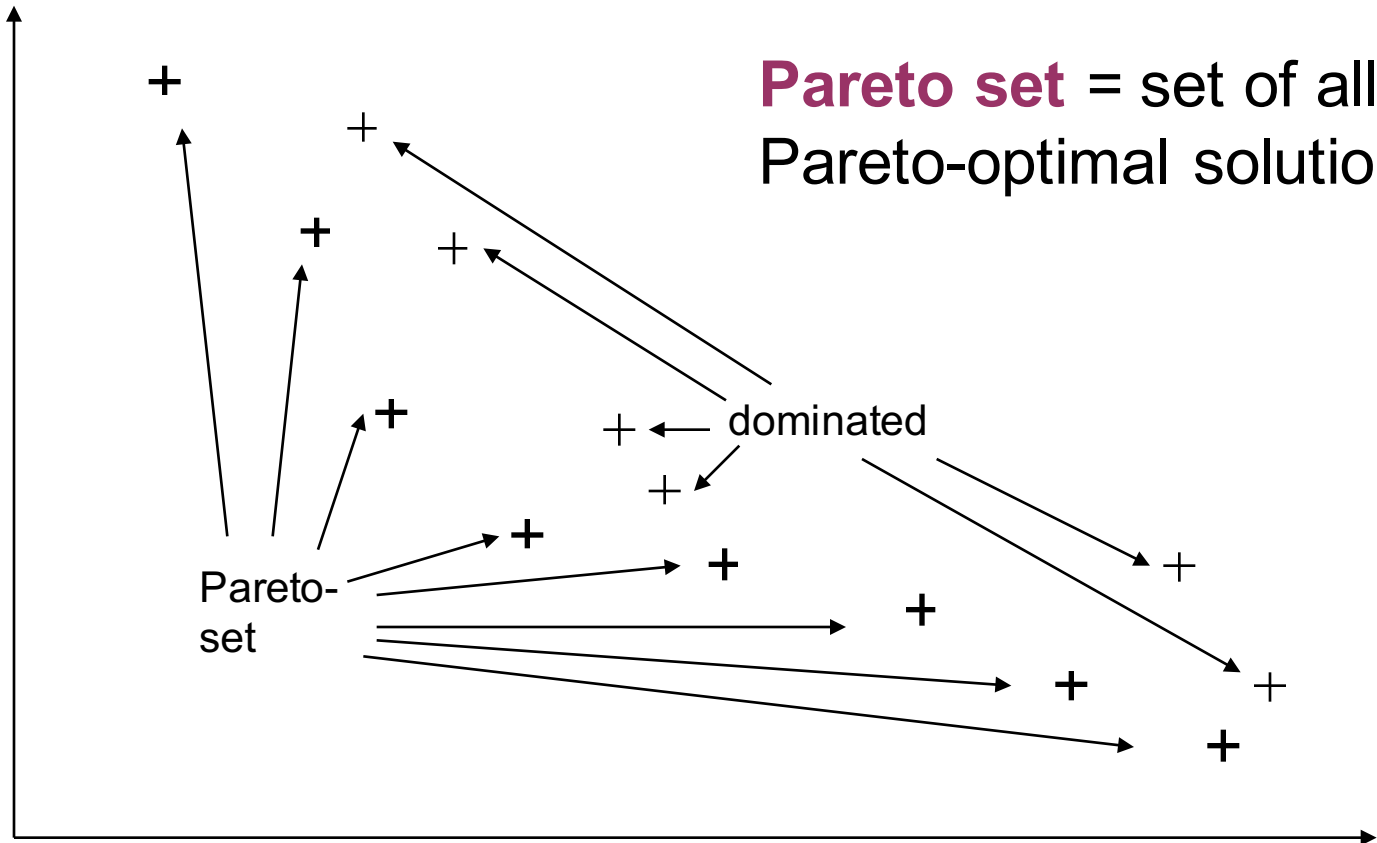
Objective 2  
(e.g. run time)

(Assuming *minimization* of objectives)



# Pareto Set

Objective 1  
(e.g. energy consumption)



**Pareto set** = set of all  
Pareto-optimal solutions

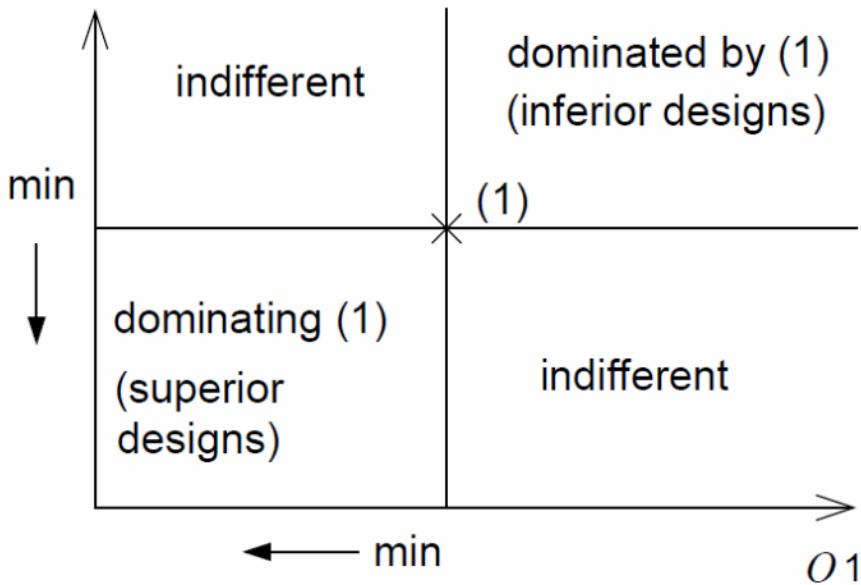
(Assuming *minimization* of objectives)

Objective 2  
(e.g. run time)

# One more time ...

## Pareto point

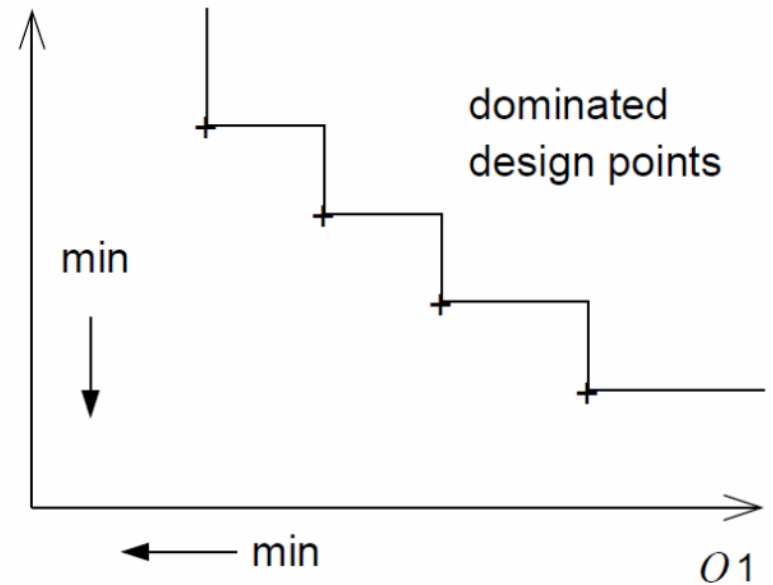
$O_2$  (e.g. memory space)



(e.g. energy)

## Pareto front

$O_2$  (e.g. memory space)



(e.g. energy)

# Design space evaluation

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**Design space evaluation** (DSE) based on Pareto-points is the process of finding and returning a set of Pareto-optimal designs to the user, enabling the user to select the most appropriate design.

# How to evaluate designs according to multiple criteria?

Many different criteria are relevant for evaluating designs:

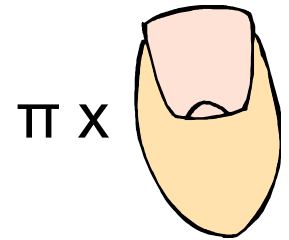
- Average & worst case delay
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How to compare different designs?  
(Some designs are “better” than others)

# Average delays (execution times)

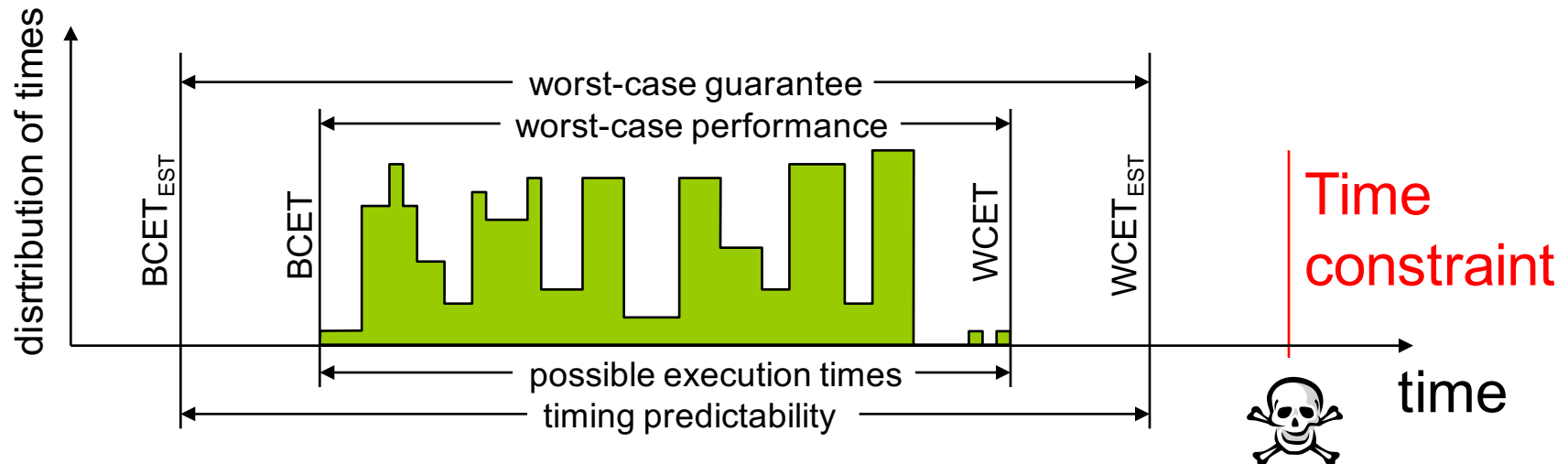
- **Estimated** average execution times :  
Difficult to generate sufficiently precise estimates;  
Balance between run-time and precision
- **Accurate** average execution times:  
As precise as the input data is.



We need to compute **average** and **worst case** execution times

# Worst case execution time (1)

Definition of worst case execution time:



WCET<sub>EST</sub> must be

1. safe (i.e.  $\geq$  WCET) and
2. tight ( $WCET_{EST} - WCET \ll WCET_{EST}$ )

# Worst case execution times (2)

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## Complexity:

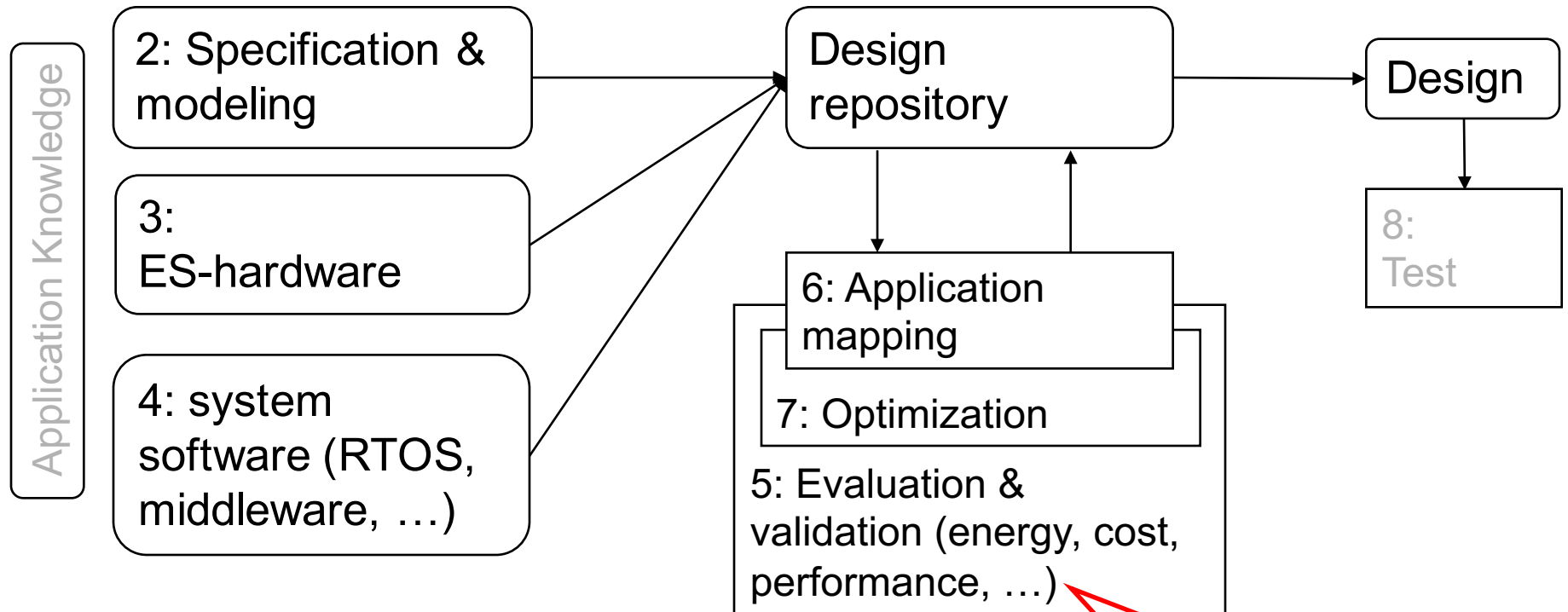
- in the general case: undecidable if a bound exists.
- for restricted programs: simple for “old” architectures, very complex for new architectures with pipelines, caches, interrupts, virtual memory, etc.



## Approaches:

- for hardware: requires detailed timing behavior
- for software: requires availability of machine programs; complex analysis (see, e.g., [www.absint.de](http://www.absint.de))

# Structure of this course



["Appendix": Standard Optimization Techniques]

Numbers denote sequence of chapters



# Integer linear programming models

Ingredients:

- Cost function
  - Constraints
- } Involving linear expressions of integer variables from a set  $X$

Cost function  $C = \sum_{x_i \in X} a_i x_i$  with  $a_i \in \mathbb{R}, x_i \in \mathbb{N}$  (1)

Constraints:  $\forall j \in J : \sum_{x_i \in X} b_{i,j} x_i \geq c_j$  with  $b_{i,j}, c_j \in \mathbb{R}$  (2)

**Def.:** The problem of minimizing (1) subject to the constraints (2) is called an **integer linear programming (ILP) problem**.

If all  $x_i$  are constrained to be either 0 or 1, the ILP problem is said to be a **0/1 integer linear programming problem**.

# Example

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$$C = 5x_1 + 6x_2 + 4x_3$$

$$x_1 + x_2 + x_3 \geq 2$$

$$x_1, x_2, x_3 \in \{0,1\}$$

$x_1$	$x_2$	$x_3$	$C$
0	1	1	10
1	0	1	9
1	1	0	11
1	1	1	15

← Optimal

# Remarks on integer programming

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- Maximizing the cost function: just set  $C' = -C$
- Integer programming is NP-complete.
- Running times depend exponentially on problem size, but problems of  $>1000$  vars solvable with good solver (depending on the size and structure of the problem)
- The case of  $x_i \in \mathbb{R}$  is called *linear programming* (LP). Polynomial complexity, but most algorithms are exponential, in practice still faster than for ILP problems.
- The case of some  $x_i \in \mathbb{R}$  and some  $x_i \in \mathbb{N}$  is called *mixed integer-linear programming*.
- ILP/LP models good starting point for modeling, even if heuristics are used in the end.
- Solvers: lp\_solve (public), CPLEX (commercial), ...

# An Example: Knapsack Problem

Example IP formulation:

The Knapsack problem:

I wish to select items to put in my backpack.

There are  $m$  items available.

Item  $i$  weights  $w_i$  kg,

Item  $i$  has value  $v_i$ .

I can carry  $Q$  kg.

$$\text{Let } x_i = \begin{cases} 1 & \text{if I select item } i \\ 0 & \text{otherwise} \end{cases}$$

$$\max \sum_i x_i v_i$$

$$\text{s.t. } \sum_i x_i w_i \leq Q$$

$$x_i \in \{0,1\}, \forall i$$

# Variance of Knapsack Problem

- **Given** a set of periodic tasks with implicit deadlines
  - Task  $\tau_i$ : period  $T_i$ ,
    - Options: Execution without/with scratchpad memory (SPM)
    - Without SPM: Worst-case execution time  $C_{i,1}$
    - With SPM: required  $m_i$  scratchpad memory size and Worst-case execution time  $C_{i,2}$
    - Utilization without SPM  $U_{i,1} = C_{i,1}/T_i$
    - Utilization with SPM is  $U_{i,2} = C_{i,2}/T_i$

- **Objective**

- Select the tasks to be put into the SPM
- Minimize the required SPM size
- The utilization of the task set should be no more than 100%

$$\begin{aligned} \min \quad & \sum_i x_i m_i \\ \text{s.t.} \quad & \sum_i x_i U_{i,2} + \sum_i (1 - x_i) U_{i,1} \leq 1 \\ & x_i \in \{0,1\}, \quad \forall i \end{aligned}$$

# Summary

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## Integer (linear) programming

- Integer programming is NP-complete
- Linear programming is faster
- Good starting point even if solutions are generated with different techniques

## Simulated annealing

- Modeled after cooling of liquids
- Overcomes local minima

## Evolutionary algorithms

- Maintain set of solutions
- Include selection, mutation and recombination

# Evolutionary Algorithms (1)

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- **Evolutionary Algorithms** are based on the collective learning process within a population of individuals, each of which represents a search point in the space of potential solutions to a given problem.
- The population is arbitrarily initialized, and it evolves towards better and better regions of the search space by means of randomized processes of
  - **selection** (which is deterministic in some algorithms),
  - **mutation**, and
  - **recombination** (which is completely omitted in some algorithmic realizations).

[Bäck, Schwefel, 1993]

# Evolutionary Algorithms (2)

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- *The environment (given aim of the search) delivers a quality information (**fitness value**) of the search points, and the selection process favours those individuals of higher fitness to reproduce more often than worse individuals.*
- *The recombination mechanism allows the mixing of parental information while passing it to their descendants, and mutation introduces innovation into the population*

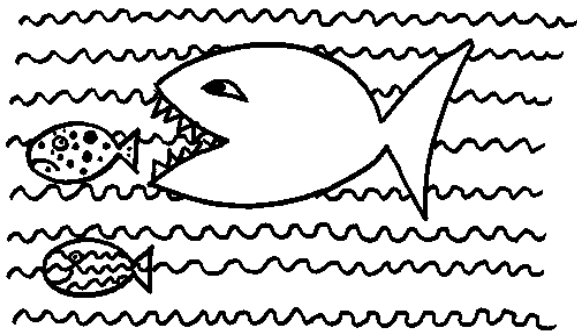
[Bäck, Schwefel, 1993]



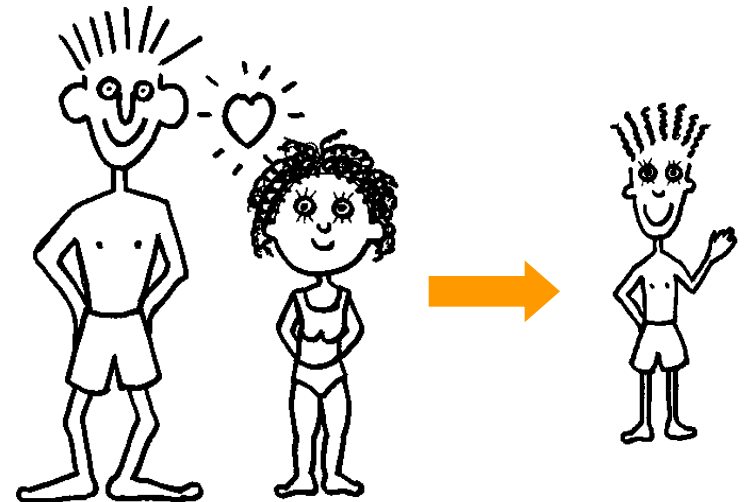
# Evolutionary Algorithms

## Principles of Evolution

### ① Selection



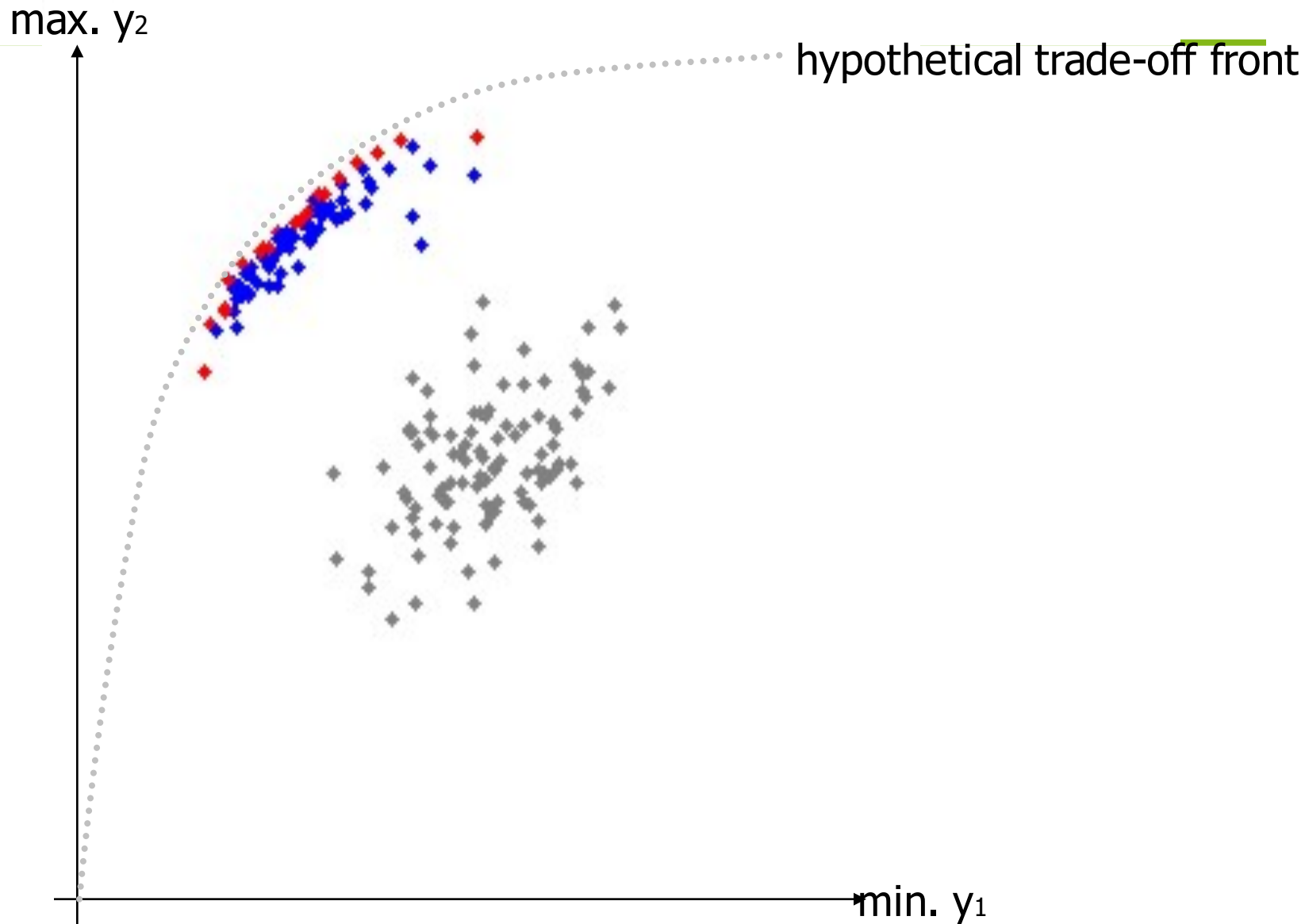
### ③ Cross-over



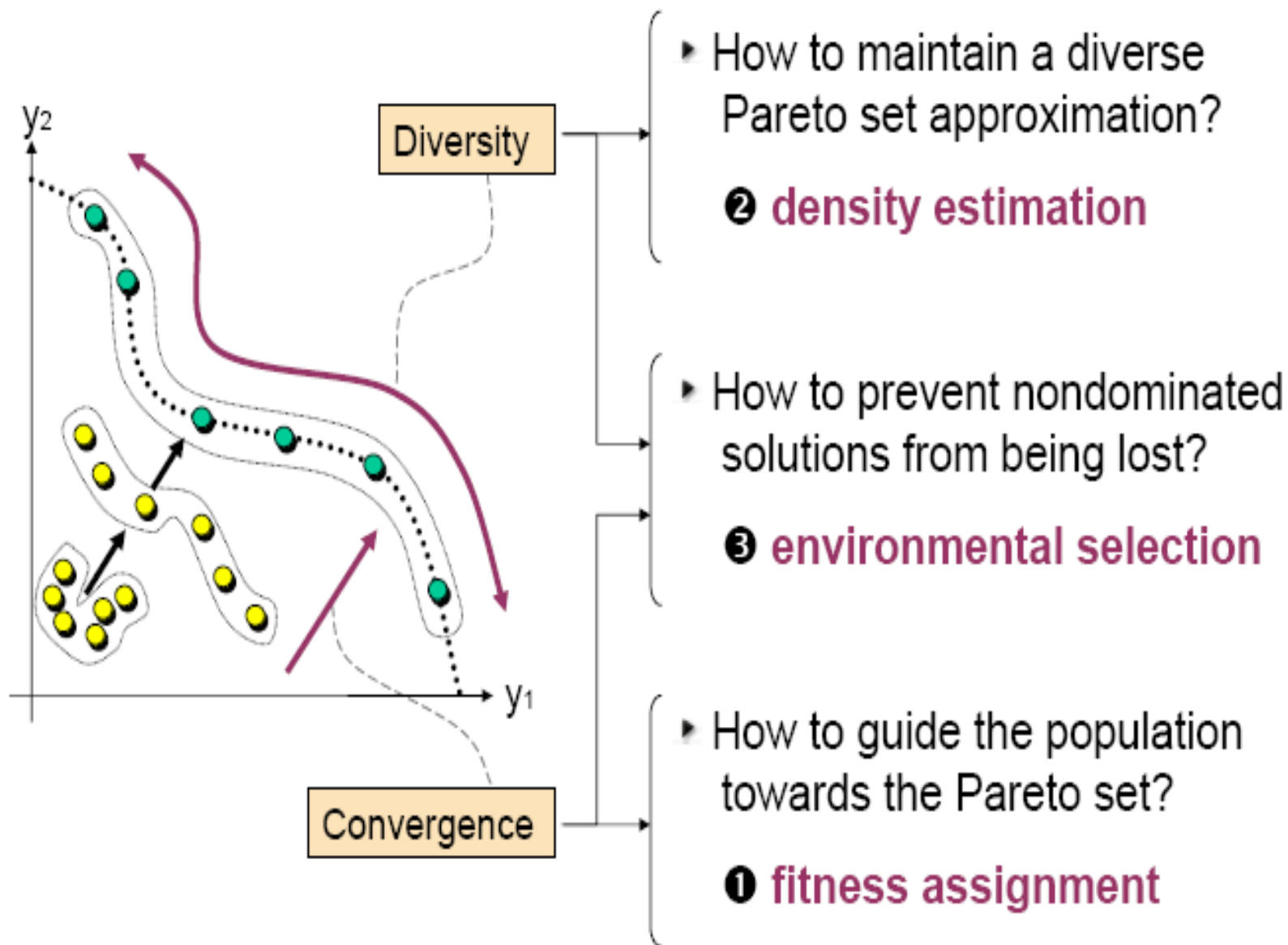
### ② Mutation



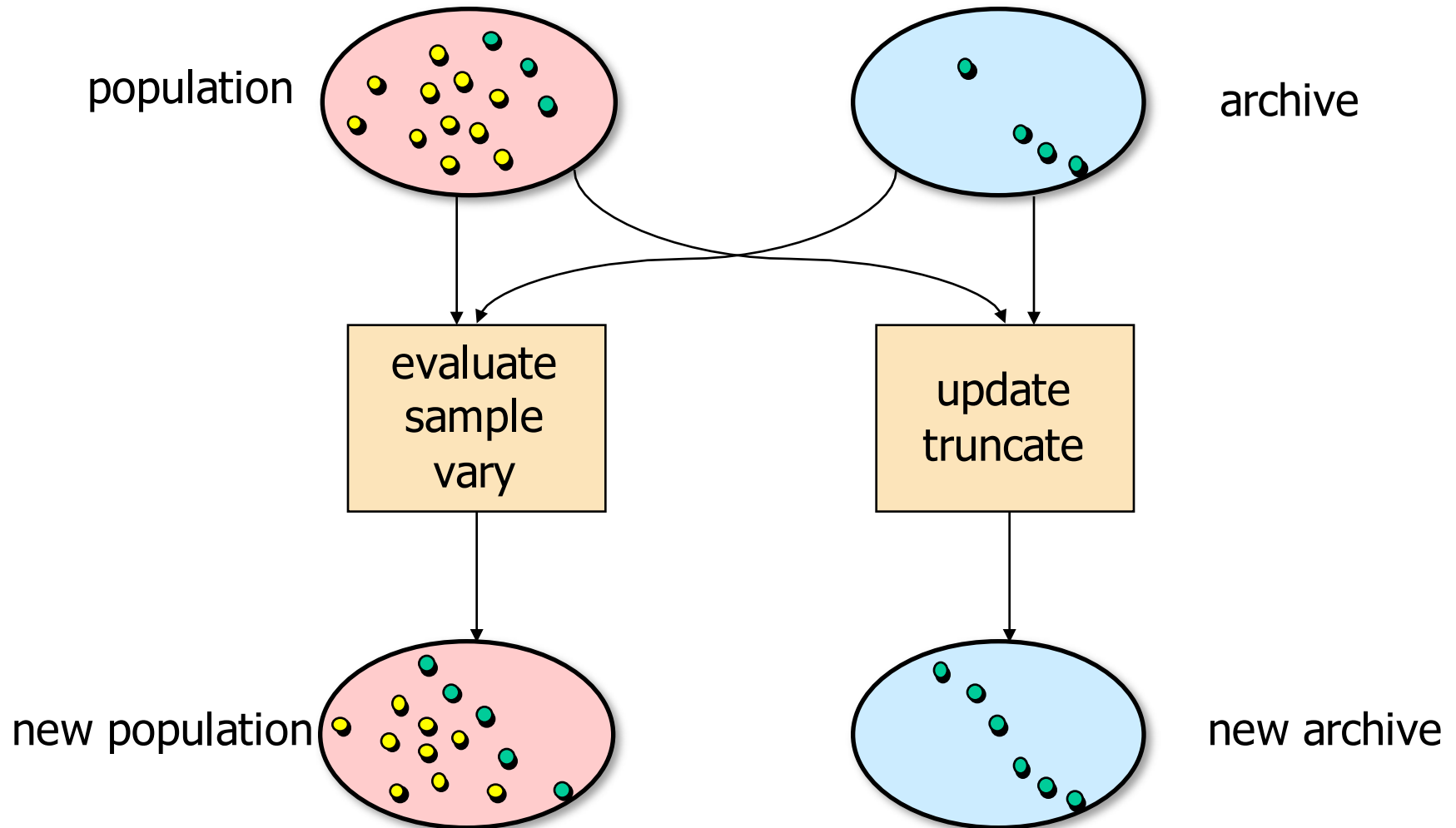
# An Evolutionary Algorithm in Action



# Issues in Multi-Objective Optimization



# A Generic Multiobjective EA



# Example: SPEA2 Algorithm

- |                |   |
|----------------|---|
| <i>Step 1:</i> | Generate initial population $P_0$ and empty archive (external set) $A_0$ . Set $t = 0$ .  |
| <i>Step 2:</i> | Calculate fitness values of individuals in $P_t$ and $A_t$ .  |
| <i>Step 3:</i> | $A_{t+1}$ = nondominated individuals in $P_t$ and $A_t$ .<br>If size of $A_{t+1} > N$ then reduce $A_{t+1}$ , else if size of $A_{t+1} < N$ then fill $A_{t+1}$ with dominated individuals in $P_t$ and $A_t$ . |
| <i>Step 4:</i> | If $t > T$ then output the nondominated set of $A_{t+1}$ .<br>Stop.   |
| <i>Step 5:</i> | Fill mating pool by binary tournament selection.  |
| <i>Step 6:</i> | Apply recombination and mutation operators to the mating pool and set $P_{t+1}$ to the resulting population. Set $t = t + 1$ and go to Step 2.  |

# *Simulated Annealing*

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- General method for solving combinatorial optimization problems.
- Based the model of slowly cooling crystal liquids.
- Some configuration is subject to changes.
- Special property of Simulated annealing: Changes leading to a poorer configuration (with respect to some cost function) are accepted with a certain probability.
- This probability is controlled by a temperature parameter: the probability is smaller for smaller temperatures.

# Simulated Annealing Algorithm

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```
procedure SimulatedAnnealing;  
var i, T: integer;  
begin  
  i := 0; T := MaxT;  
  configuration := <some initial configuration>;  
  while not terminate(i, T) do  
    begin  
      while InnerLoop do  
        begin NewConfig := variation(configuration);  
          delta := evaluation(NewConfig, configuration);  
          if delta < 0  
            then configuration := NewConfig;  
            else if SmallEnough(delta, T, random(0,1))  
              then configuration := Newconfiguration;  
        end;  
      T := NewT(i, T); i := i + 1;  
    end; end;
```

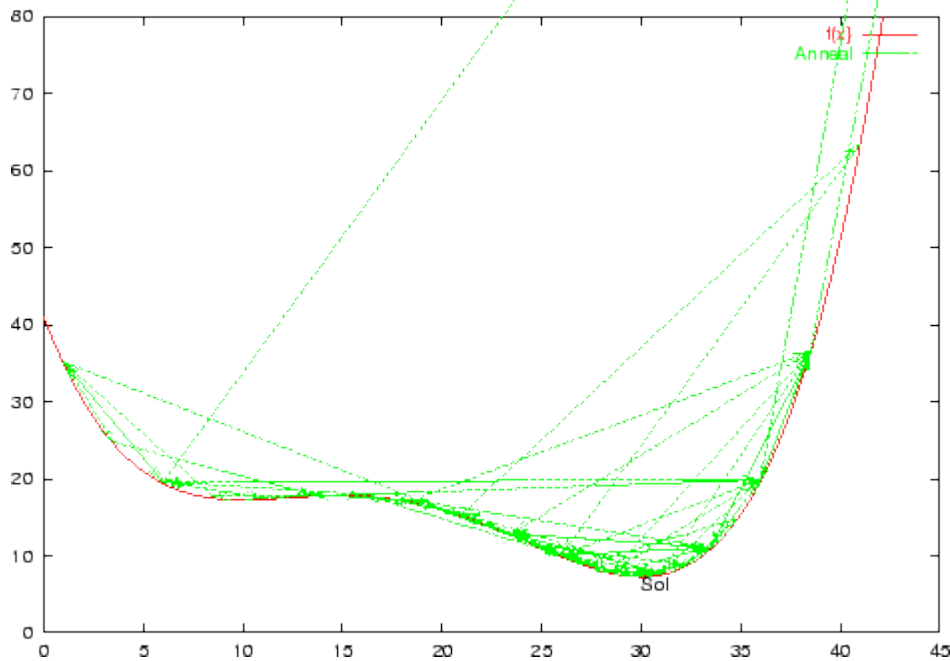
# Explanation

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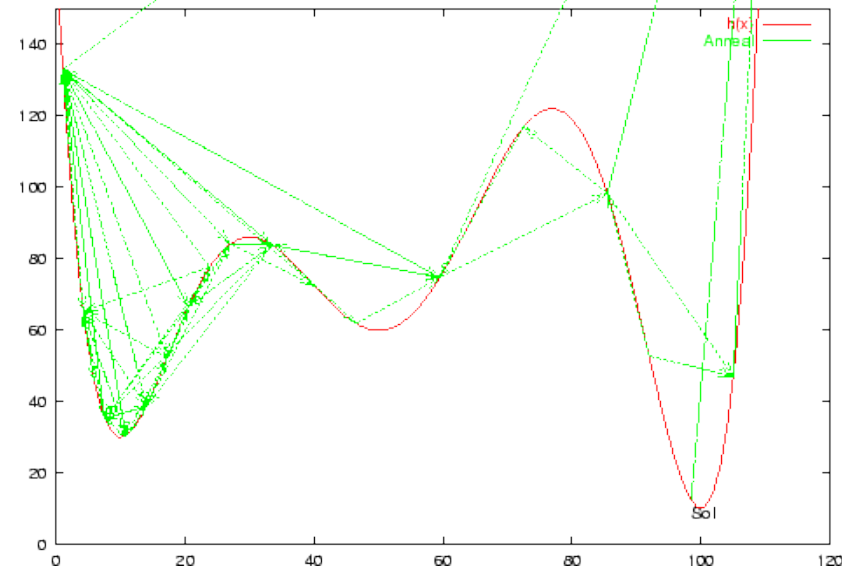
- Initially, some random initial configuration is created.
- Current temperature is set to a large value.
- Outer loop:
  - Temperature is reduced for each iteration
  - Terminated if (temperature  $\leq$  lower limit) or (number of iterations  $\geq$  upper limit).
- Inner loop: For each iteration:
  - New configuration generated from current configuration
  - Accepted if (new cost  $\leq$  cost of current configuration)
  - Accepted with temperature-dependent probability if (cost of new config.  $>$  cost of current configuration).



# Behavior for actual functions



130 steps



200 steps

[[people.equars.com/~marco/poli/phd/node57.html](http://people.equars.com/~marco/poli/phd/node57.html)]

<http://foghorn.cadlab.lafayette.edu/cadapplets/fp/fplIntro.html>

# Performance

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- This class of algorithms has been shown to outperform others in certain cases [Wegener, 2005].
- Demonstrated its excellent results in the TimberWolf layout generation package [Sechen]
- Many other applications ...

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